

1 Bias correction that addresses frequency dependence
2 and preserves model-predicted mean changes

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23 **Abstract**

24 Global climate model temperature and precipitation fields need to be corrected for biases
25 relative to observations before they can be used for climate change impact studies. Three existing
26 bias correction methods, and a new one developed here, are applied to daily maximum
27 temperature and precipitation from 21 climate models to investigate: 1) How bias correction
28 alters the climate change signal of the original model; 2) How different methods affect model
29 biases in the simulation of variance as a function of frequency. Quantile mapping (QM) and
30 cumulative distribution function transform (CDF-t) bias correction can significantly alter the
31 signal of change from the original climate model, with differences of up to 2°C and 30
32 percentage points for monthly temperature and precipitation, respectively. Equidistant quantile
33 matching (EDCDFm) preserves model-predicted changes in daily maximum temperature, but
34 alters model-predicted changes in precipitation by up to 30 percentage points in some locations.
35 An extension to EDCDFm termed PresRat is introduced, which generally preserves the original
36 model-predicted changes in precipitation by operating on ratios instead of differences, using a
37 precipitation threshold to make the fraction of model zero-precipitation days match observations,
38 and incorporating a final correction factor. Additionally, a frequency-dependent bias correction
39 method is introduced that is twice as effective as standard bias correction in reducing errors in
40 the models' simulation of variance as a function of frequency, and (unlike standard bias
41 correction) does so while making very few locations worse.

42

43 **1. Introduction**

44 Global climate models (GCMs) are being used to explore an ever widening set of
45 problems, some of which are sensitive to biases in the model simulated fields (IPCC, 2007). For
46 example, daily precipitation biases can have a detrimental effect on hydrological simulations due
47 to the non-linear nature of runoff; a moderate amount of precipitation generates little runoff if the
48 soil is able to absorb the moisture, while doubling the precipitation might exceed the moisture
49 storage capacity of the soil and generate much more than twice as much runoff. This non-linear
50 relationship becomes more extreme in arid regions (Wigley and Jones, 1985), intensifying the
51 sensitivity of runoff to GCM precipitation biases. Likewise, significant biases in surface
52 humidity and evapotranspiration can arise from relatively small temperature biases due to the
53 nonlinear nature of the Clausius-Clapyron equation. Unfortunately, the detrimental impacts of
54 climate model biases on a non-linear system are not straightforward to remove.

55 For this reason hydrological simulations generally bias correct GCM output fields before
56 they are used. Corrected variables include temperature and precipitation, and sometimes other
57 relevant quantities such as downward solar radiation, humidity, or wind speed. Bias correction is
58 often an integral part of a downscaling scheme that takes account of large scale GCM biases as
59 well as topographical and other effects that operate at a finer scale than can be resolved by a
60 GCM (e.g., Wood et al. 2002; Maurer et al. 2010). Here however we consider the bias correction
61 step alone. Maraun (2013) has pointed out that bias correction is most straightforwardly applied
62 on a spatial scale that is near the original GCM's spatial resolution, so we restrict our attention to
63 bias correction on a grid commensurate with the original GCMs.

64 One common form of bias correction is quantile mapping (QM; e.g., Panofsky and Brier
65 1968; Wood et al. 2002; Thrasher et al. 2012), which adjusts a simulated climate variable (e.g.

66 temperature or precipitation) at a given location by mapping the quantiles of the simulated
67 distribution onto the quantiles of the observations at that location. QM has been widely applied
68 to climate model output over the U.S. (e.g., Maurer et al. 2007, 2014) and globally (Thrasher et
69 al. 2012). QM alters both the model's mean and temporal variability, bringing them into
70 agreement with observations over some common historical period. Gudmundsson et al. (2012)
71 evaluate different ways of implementing QM and find that relatively straightforward non-
72 parametric methods, such as used here, perform well compared to more complicated schemes.

73 Previous studies have shown that QM tends to alter the original GCM's projected trend
74 (Hagemann et al. 2011; Pierce et al. 2013; Maurer and Pierce 2013). Whether this is a desirable
75 feature is a research question not addressed here. However, this property certainly engenders
76 confusion and inconsistent results, for example between bias corrected regional climate studies
77 and GCM results assessed by the IPCC (2007, 2013). If a climate model has too much variability
78 then QM tends to reduce variability on all timescales, suppressing the original trend. If the GCM
79 has too little variability, QM tends to increase the trend along with variability on shorter
80 timescales. As bias correction is a purely statistical method it fails to discriminate between the
81 physical processes determining trends associated with anthropogenic forcing and shorter-term
82 fluctuations associated with natural internal climate variability. From this perspective there is
83 little justification for allowing bias correction that primarily addresses problems on synoptic,
84 seasonal and annual timescales to change the trend as well.

85 Some previous schemes have addressed the problem of bias correction altering GCM-
86 projected trends. For example, the BCSD method (Wood et al. 2002) removes temperature trends
87 over the period to be downscaled, bias corrects and then downscales the anomalies to a fine grid,
88 then adds back in the original GCM trend fields interpolated to the fine grid. Although

89 straightforward and useful, this approach has the drawback that the final trend is, to first order,
90 merely the interpolated GCM trend. This is confusing to end users who might reasonably expect
91 that the downscaled trend will reflect more than simply the interpolated GCM trend, and means
92 that the spatial structure of the trend is not necessarily commensurate with the spatial structure of
93 the daily, monthly, or annual variability. In this work we address this limitation by constructing a
94 bias correction method that retains the model-predicted change in the first place. The bias
95 corrected fields can then be downscaled, and the final trend in the downscaled fields will be
96 affected by the downscaling process rather than being independent of it. Pierce and Cayan (2013)
97 addressed this issue by partitioning their future model runs into 30-yr segments (2010-2039,
98 etc.), downscaling each segment with respect to its own climatology, then separately
99 downscaling the global model predicted *change* in climatology in each segment and adding it
100 back in. This preserves model changes on timescales longer than 30 years but allows shorter
101 timescale changes to be bias corrected. The work here is more widely applicable since it is a self-
102 contained bias correction method that preserves model-predicted changes without reference to
103 how subsequent downscaling handles the trend. As such it is potentially applicable to
104 downscaling methods where separately downscaling the model-predicted change is not desirable
105 or viable.

106 Addressing the trend is not the only issue relevant to climate impact studies. The
107 approaches used in BCSD and by Pierce and Cayan (2013) treat the trend differently from other
108 timescales during the bias correction process. Yet a GCM may have too much variability on, for
109 instance, synoptic timescales of 2-10 days but too little variability on the annual timescale.
110 Neither a simple quantile based bias correction nor the approaches noted above address this
111 problem. Misrepresentation of variance as a function of frequency could influence a simulation

112 of heat waves or flooding events, while distortions in the relative importance of synoptic scale
113 versus interannual variability could affect agriculture and ecosystems. Inaccurate partitions
114 between short- and long-timescale precipitation variability could affect simulations of droughts
115 and reservoir storage since the hydrological and ecological result of a given amount of annual
116 precipitation varies greatly depending on whether the precipitation is delivered equally
117 throughout the year or very unevenly, with a strong contrast between wet and dry seasons.

118 While the CMIP5 GCM simulations appear to have improved in these regards relative to
119 prior simulations, such biases can still be substantial (Sillmann et al. 2013). Lower frequency
120 variability in the climate system, such as El Niño-Southern Oscillation (ENSO), with an
121 observed period of 2-7 years, are also imperfectly simulated by GCMs (e.g., Bellenger et al.,
122 2013; Collins et al., 2013), as are the teleconnections that can drive regional precipitation and
123 temperature variability (Sheffield et al., 2013). Since natural variability in observations and
124 historical GCM simulations is not synchronized (e.g., Eden et al., 2012), where regional climate
125 is influenced by low-frequency variability the biases in GCM climate output also can be
126 expected to mimic this natural variability, which has been noted in GCM climate simulations
127 over the U.S. (e.g., Maurer et al., 2013). A correction of GCM output to account for biases in
128 variability on different timescales is warranted where impacts are sensitive to this variability, and
129 has not yet been attempted.

130 Our first goal is to document how existing bias correction schemes alter the projected
131 climate changes obtained from GCMs. We then propose a method that preserves the model-
132 projected changes. Third, we document model biases as a function of frequency so that the
133 locations and extent to which this is a problem in current state-of-the-art GCMs can be
134 understood. Ault et al. (2012) examined model biases at the interannual and decadal timescales,

135 however we find that bias correction is sensitive to misrepresented variability on shorter
136 timescales as well. Lastly, we present a frequency-dependent bias correction scheme that reduces
137 the problem of frequency-dependent model biases. Maurer et al. (2013) have already
138 demonstrated how model biases can vary over time and at extreme percentiles; this work adds to
139 that list by showing that there are biases in variance at different frequencies.

140 The rest of this report is structured as follows. In section 2 we describe the observed and
141 model data sources. Section 3 addresses the problem of bias correction altering model-predicted
142 changes, shows the extent to which this happens, and proposes a bias correction scheme that
143 preserves model-predicted mean future changes. Section 4 addresses frequency-dependent model
144 biases, documents the extent to which these are seen in the current generation of global climate
145 models, and proposes a method for correcting these biases. The interaction of frequency-
146 dependent bias correction with standard bias correction is also addressed. A summary and
147 conclusions are given in section 5.

148 **2. Data sources and time periods**

149 **2.1 Global climate models**

150 We use daily maximum temperature and precipitation fields from 21 GCMs that
151 participated in the Coupled Model Intercomparison Project, version 5 (CMIP5; Taylor et al.,
152 2012), listed in Table 1. The models used are all those available from the U.S. Bureau of
153 Reclamation (USBR) archive of regrided ($1^\circ \times 1^\circ$ longitude-latitude) CMIP5 global climate
154 models at the time this work was performed ([ftp://gdo-](ftp://gdo-dcp.ucllnl.org/pub/dcp/archive/cmip5/bcca)
155 [dcp.ucllnl.org/pub/dcp/archive/cmip5/bcca](ftp://gdo-dcp.ucllnl.org/pub/dcp/archive/cmip5/bcca); Maurer et al. 2014). Using the USBR regrided data
156 has several advantages. It means we can build on work already done to obtain the raw climate

157 model fields and regrid the disparate climate model grids to a uniform representation.
158 Additionally, starting from the same regridded data as the USBR archive uses ensures that later
159 work using the bias corrected fields generated here can be directly compared to the existing
160 USBR archive results.

161 Historical-data are available over the period 1950-2005. Future changes over the period
162 2006-2099 are simulated using model output from representative concentration pathway 8.5
163 (RCP8.5) experiments, which correspond to a relatively high emissions scenario (van Vuuren et
164 al. 2011).

165 **2.2 Observations**

166 We used observed daily maximum temperature and precipitation data from Maurer et al.
167 (2002), as updated through 2010 (available from
168 http://www.engr.scu.edu/~emaurer/gridded_obs/index_gridded_obs.html). The ultimate source
169 of this gridded product is the NOAA co-operative observer weather stations, with techniques
170 from the PRISM project (Daly et al. 1994) used to augment observed precipitation values in
171 sparsely instrumented locations. The data are provided on a $1/8^\circ \times 1/8^\circ$ latitude-longitude grid,
172 which was aggregated to the same $1^\circ \times 1^\circ$ grid as the global climate model outputs.

173 **2.3 Time periods used**

174 The World Meteorological Organization (WMO) recommends that climatological
175 normals be calculated over 30-year periods (a brief history of climatological normals can be
176 found in Trewin 2007). The U.S. National Oceanic and Atmospheric Administration (NOAA)
177 and National Climatic Data Center (NCDC) do the same (e.g.,
178 <http://www.ncdc.noaa.gov/oa/climate/normals/usnormals.html>). We follow this guidance by bias
179 correcting GCM values to a 30-yr climatological record of observations, and furthermore by bias

180 correcting contiguous 30-yr segments of climate simulations individually. For the future model
181 projections we bias correct the periods 2010-2039, 2040-2069, and 2070-2099 separately. In the
182 results shown below we focus on 2070-2099 as our “future” period. The climatological
183 (historical) period is the last 30 years of the GCMs’ historical runs (1976-2005), used for both
184 the models and observations.

185 **3. Preserving model-predicted mean changes**

186 **3.1 Overview**

187 In this section we first evaluate the ability of three existing bias correction methods to
188 preserve GCM-predicted future changes in daily maximum temperature and precipitation. We
189 then propose a modification to an existing bias correction method for precipitation that preserves
190 model-predicted mean future changes.

191 Both temperature and precipitation are examined because they have different spectral
192 characteristics and we evaluate their changes in two contrasting ways: as a difference with
193 temperature (future – historical) but as a ratio with precipitation (future / historical). This is
194 unlike the analysis in Maurer and Pierce (2013), which evaluated precipitation changes as a
195 difference. However, it can be useful to evaluate precipitation changes as a ratio since GCMs
196 may have significant biases in precipitation for a variety of reasons including the inability to
197 adequately resolve topography and its effect on precipitation, for example often extending
198 mountain precipitation too far into a rain shadow. In certain regions and seasons model biases
199 may be several times the local observed climatology, making it sensible to consider model
200 changes as fractional changes relative to the model’s own base climatology rather than as
201 differences that are subsequently applied to observed climatology.

202 In the results shown here all the bias correction techniques are applied to daily values
203 within each month (i.e., all days in January are bias adjusted together, then all days in February,
204 etc.) to account for the cyclostationary nature of climate fields. More sophisticated treatments of
205 this aspect of bias correction can be found in, for example, Piani et al. (2010), Abatzoglou and
206 Brown (2011), and Thrasher et al. (2012). The historical period is 1976-2005 and the future
207 period is 2070-99.

208 **3.2 Effect of quantile mapping on model-predicted changes**

209 In quantile mapping (QM; Wood et al. 2002) a raw GCM value x is converted to a bias
210 corrected value \hat{x} according to

$$\hat{x} = F_{sh}^{-1} \left(F_{gh}(x) \right) \quad (1)$$

211 where, using the notation from Michelangeli et al. 2009, $F(x)$ is the quantile of value x in the
212 cumulative distribution function (CDF), $F^{-1}(u)$ is the value in a CDF of quantile u , the first
213 subscript is s for the station (observed) values and g for the GCM (model) values, and the second
214 subscript is h for the historical time period. Thus, QM bias corrects a model value by changing it
215 to the observed value at the quantile that the model value falls in the model's historical
216 distribution. The process is illustrated schematically, using CDFs of synthetic gamma
217 distributions to mimic precipitation data, in Figure 1a and the caption thereof. Values off the end
218 of the distribution are handled as described in Wood et al. (2002), i.e. by fitting a Gumbel
219 extreme value distribution to the precipitation values and a Gaussian distribution to the
220 temperature values.

221 QM has difficulty bias-correcting precipitation if the GCM has more zero-precipitation
222 days than observed since there is no obvious prescription to determine which of the model's too
223 numerous zero precipitation days should be assigned a non-zero value. If zero precipitation

224 remains on these days, the QM bias-corrected time series will have a smaller mean value than
225 observed. However, in practice current GCMs generally have too few zero precipitation values,
226 sometimes referred to as the drizzle problem (e.g., Sun et al. 2006, Dai 2006).

227 QM's tendency to alter GCM-simulated trends (as noted in the introduction) was not
228 relevant to early applications of QM in hydrological modeling, such as in Wood et al. (2002),
229 which developed and applied QM in the context of seasonal forecasting. When lead times are on
230 the order of a year or less there is no reason to assume a significant shift in the model
231 distributions over the forecast period, so the behavior of QM when the mean changes appreciably
232 was not examined. This is consistent with the fact that Eq. 1 uses only historical information, not
233 referring to the future model-projected distributions in any way. Despite this, QM has frequently
234 been applied to climate change simulations where the mean does change appreciably, for
235 example in multi-decade climate simulations that include anthropogenic changes in greenhouse
236 gasses and aerosol forcing (e.g., Harding et al. 2012).

237 The tendency for QM to alter model-projected changes is illustrated with the CCSM4
238 GCM using July daily maximum temperature in Figure 2 and December daily precipitation in
239 Figure 3. Bias correction is applied and model-predicted changes computed using a historical
240 (1976-2005) and future period (2070-2099). Note that some fraction of variance over the future
241 period might arise from the anthropogenically forced trend. The monthly average change
242 between the future and historical periods is computed as a difference for temperature (future –
243 historical) and a ratio for precipitation (future / historical). The top row (right panel) of Figure 2
244 shows that QM decreases the model-predicted July daily maximum temperature change by more
245 than 2°C in parts of Texas, Florida, and the Southeastern states, and increases it by a similar
246 amount along the California coast. Similarly, Figure 3 shows that QM increases the model-

247 predicted change in December precipitation by 30 percentage points over parts of the Northern
248 Sierra Nevada and Rockies. Smaller changes can also be seen over the upper Midwest and
249 Southeastern states.

250 Recently, two bias correction methods have been developed that make specific choices
251 for how model-predicted future changes should be treated: the CDF-transform method (“CDF-t”;
252 Michelangeli et al. 2009) and equidistant quantile matching (“EDCDFm”; Li et al. 2010). We
253 next examine these methods to determine whether they preserve GCM-predicted mean changes
254 in temperature and precipitation. As in Maurer and Pierce (2013) we simplify by focusing
255 primarily on the model-predicted change in median value instead of the mean, although it should
256 be kept in mind that changes evaluated in different ways, for example by a least-square trend, are
257 affected by the entire distribution rather than just the change in median, and trends may differ at
258 different quantiles.

259 **3.3 The effect of EDCDFm bias correction on model-predicted changes**

260 EDCDFm (Li et al. 2010) bias corrects a future value x that falls at quantile u in the
261 future distribution by adding the historical value at u to the model predicted change in value at u :

$$\hat{x} = F_{sh}^{-1} \left(F_{gf}(x) \right) + x - F_{gh}^{-1} \left(F_{gf}(x) \right) \quad (2)$$

262 Where variables are defined as in Eq. 1 and the subscript f is for the future time period. The
263 process is illustrated schematically in Figure 1b and the caption thereof. When bias correcting a
264 historical run, so that $F_{gf} \equiv F_{gh}$, Eq. 2 reduces to Eq. 1. By definition Eq. 2 preserves the GCM-
265 predicted future change in median value as long as the change is evaluated additively. EDCDFm
266 does not necessarily preserve the model-predicted change in the mean (as opposed to median)
267 since the quantile at which the mean falls can change if the shape of the distribution changes in
268 the future. This does happen; for example, we find that for daily maximum temperature in the

269 CMIP5 models, changes in the quantile at which the mean falls can be 0.1 or more by the end of
270 this century. However, for daily maximum temperature GCM-predicted changes are generally a
271 weak function of quantile in the neighborhood of the mean value, so EDCDFm preserves the
272 model-predicted change in mean value typically to within a few hundredths of a degree C (e.g.,
273 second row of Figure 2). Considering model uncertainty and natural variability this small
274 discrepancy is irrelevant for our applications, but this should be re-evaluated if EDCDFm is
275 applied to another climate variable that undergoes less uniform changes as a function of quantile
276 or more exaggerated changes in the shape of the distribution, which could imply larger changes
277 in the quantile of the mean.

278 As formulated by Li et al. (2010) and seen in Eq. 2, EDCDFm is an additive bias
279 correction method that preserves model-predicted differences (as opposed to ratios), which is
280 appropriate for temperature. As expected, Eq. 2 does not generally preserve a GCM-predicted
281 fractional changes, i.e., $(\text{future model value} - \text{historical model value})/(\text{historical model value})$.
282 At every quantile standard EDCDFm preserves the numerator of this ratio by definition, but in
283 the process of bias correction substitutes the observed value for the historical model value in the
284 denominator, changing the ratio. This is illustrated in the second row of Figure 3. When
285 evaluated multiplicatively using precipitation, EDCDFm alters the model-predicted change by
286 more than 30 percentage points over much of the North/Central U.S. This will happen
287 particularly when there are both large biases and large changes in the upper quantiles of a
288 skewed precipitation distribution.

289 **3.4 The effect of CDF-t bias correction on model-predicted changes**

290 CDF-t bias correction (Michelangeli et al. 2009) finds a transformation that maps the
291 GCM cumulative distribution function (CDF) of a climate variable in the historical period to the
292 observed CDF, then applies that same mapping to the GCM's future CDF, yielding:

$$F_{sf}(x) = F_{sh} \left(F_{gh}^{-1} \left(F_{gf}(x) \right) \right). \quad (4)$$

293 Here, F_{sf} indicates the CDF of the bias corrected variable in the future. When bias correcting a
294 historical run Eq. 4 reduces to QM in general, although the treatment of values off the end of the
295 distribution (discussed further below) may come into play.

296 As Figure 1c makes clear, QM and EDCDFm change a model's value while preserving
297 its quantile (a point on the F_{gf} curve is bias corrected by moving it horizontally), while CDF-t
298 changes a model's quantile while preserving its value (a point on the F_{gf} curve is bias corrected
299 by moving it vertically). An alternative, but equivalent, explanation is that Eq. 4 preserves
300 model-predicted changes at quantiles, but unlike EDCDFm the model-predicted change that is
301 preserved is taken from a different quantile than it is applied to (EDCDFm applies the model-
302 predicted change at some quantile to that same quantile).

303 For example, consider the GCM-predicted change in median value. The EDCDFm bias
304 corrected change in the median value is equal to the model predicted change at a quantile of
305 $u=0.5$ (the median). However, the CDF-t bias corrected change in the median value is equal to
306 the model predicted change at some other quantile, $u^* \neq 0.5$. It can be shown that $u^* =$
307 $F_{gh} \left(F_{sh}^{-1}(0.5) \right)$, i.e. the percentile in the model historical distribution of the observed median
308 value. So CDF-t will only preserve model-predicted changes in the median under certain special
309 circumstances, such as when $u^* = 0.5$ (i.e., the GCM predicted the correct median over the

310 historical period in the first place) or if the model-predicted changes are the same at different
311 quantiles (a simple shift in the distribution).

312 The third rows of Figure 2 and Figure 3 show the effect of CDF-t bias correction on the
313 original GCM-predicted change in temperature and precipitation, respectively. CDF-t alters the
314 model predicted change in temperature by more than 1°C in the upper Midwest. The model-
315 predicted change in precipitation is affected less by CDF-t than by quantile mapping or
316 EDCDFm, but still can change the model prediction by more than 30 percentage points in some
317 locations. In other months the precipitation alterations due to CDF-t bias correction can be as
318 large as those found by quantile mapping and EDCDFm (not shown).

319 **3.5 Bias correction that preserves model-predicted mean changes**

320 Figure 1d, Figure 2, and Figure 3 show that the three bias correction methods considered
321 so far, QM, EDCDFm, and CDF-t, all produce reasonable appearing yet different future CDFs
322 and fields. Lacking theoretical guidance there is no obvious way to choose which method
323 produces the most correct future representation. Li et al. (2010) and Maurer and Pierce (2013)
324 use historical natural variability as a surrogate for forced changes to evaluate the quality of bias
325 correcting future changes, but as discussed in Maurer and Pierce (2013) this approach is limited
326 since natural variability does not necessarily arise from the same physical processes as
327 anthropogenically forced climate change.

328 Each future field is determined by the assumptions of the bias correction method used to
329 create it. QM assumes that the historical model error in value at a given *value* is preserved in the
330 future (arrow (2) in Figure 1a), EDCDFm assumes that the historical model error in value at a
331 given *quantile* is preserved in the future (Δ in Figure 1c), and CDF-t assumes that the historical
332 model error in *quantile* at a given quantile is preserved in the future (arrow (2) in Figure 1b).

333 (The “missing” version of this quartet of bias correction methods, which would assume that the
334 historical model error in quantile at a given *value* is preserved in the future, could also be
335 constructed.)

336 Here we explore an alternative assumption: that the GCM-predicted mean change is
337 preserved in the bias corrected future projections. The advantage of this approach is that
338 downscaled results will then be more consistent with existing GCM analyses such as IPCC
339 (2007, 2013).

340 EDCDFm already preserves model-predicted changes in temperature (evaluated
341 additively) for all practical purposes so we adopt it for temperature here. However an amended
342 form is required for precipitation since we evaluate its changes multiplicatively. Eq. 2 can be
343 recast as a multiplicative scheme that preserves the model-predicted change as a ratio:

$$\hat{x} = F_{sh}^{-1} \left(F_{gf}(x) \right) \frac{x}{F_{gh}^{-1} \left(F_{gf}(x) \right)}. \quad (3)$$

344 In other words, if the predicted GCM value x falls at quantile u , then the bias corrected
345 precipitation value is the historical value at u multiplied by the model-predicted change at u
346 evaluated as a ratio. In fact, Li et al. (2010) do this for a small number (~0.3%) of grid points that
347 otherwise are “problematic” when bias correcting precipitation additively, although in the
348 context of their study they did not explore the implications of Eq. 3 for preserving a model-
349 predicted future precipitation change. Note that Eq. 3 cannot be applied at quantiles where there
350 is no precipitation, in which case the denominator becomes zero. In this event we simply set the
351 model-predicted change ratio to 1.

352 The treatment of zero-precipitation days is an important consideration for regional
353 climate change (Polade et al. 2014). We calculate a location-specific zero-precipitation threshold
354 for the GCM, τ , such that applying τ makes the model’s number of zero-precipitation days

355 match observations over the historical period. Specifically, $\tau = F_{gh}(q_{\max})$ where q_{\max} is the largest
 356 quantile at which $F_{sh}(q_{\max}) = 0$. We require $\tau \geq 0.01$ mm/day to avoid the possibility of very
 357 small denominators in Eq. 3. Current GCMs tend to precipitate too frequently, often at daily
 358 amounts above 0.01 mm, so this limit is rarely invoked. The GCM-predicted future fraction of
 359 zero-precipitation days, Z_{gf} , is calculated using τ with the GCM's original (non-bias corrected)
 360 future time series. The model data is then bias corrected, and the smallest Z_{gf} fraction of
 361 precipitation values are set to zero. In most cases this means that the GCM-predicted change in
 362 fraction of zero-precipitation days is preserved in the bias-corrected output. However it
 363 sometimes happens that the bias-corrected future time series has a larger fraction of zero
 364 precipitation days than Z_{gf} , which is not a correctable bias since there is no way to know which
 365 zero-precipitation days should be set to have a positive value.

366 Model-predicted changes in mean precipitation (evaluated multiplicatively) are generally
 367 not preserved using Eq. 3 for the same reasons noted above for the standard additive EDCDFm
 368 technique (i.e., changes in the quantile at which the mean falls). Although this results in
 369 negligible errors in temperature, precipitation distributions tend to be more skewed than
 370 temperature distributions and GCMs can show significantly varying predictions of future change
 371 as a function of quantile. Between these two effects Eq. 3 can still alter model-predicted changes
 372 in mean precipitation in some seasons and locations.

373 The model-predicted mean precipitation change (evaluated as a ratio) over the bias
 374 correction period can be preserved exactly if the right hand side of Eq. 3 is multiplied by a
 375 correction factor K :

$$376 \quad K = \langle x \rangle / \langle \hat{x} \rangle \quad (4)$$

377 where brackets indicate time averaging over all days in the appropriate month (since we are
378 implementing bias correction separately for each month). I.e., K is the ratio of the mean change
379 in the original GCM to the mean change in the bias corrected GCM. We call the combination of
380 Eqs. 3 (the ratio-preserving formulation of EDCDFm) and 4, together with the treatment of zero-
381 precipitation days described above, the PresRat bias-correction method because it “preserves the
382 ratio,” specifically the mean GCM-predicted future precipitation change evaluated as a ratio. In
383 application the future / historic ratios are first computed at each quantile, then those ratios are
384 scaled by K . Figure 1d includes results from PresRat (purple line) applied to the synthetic
385 example data as well as the other methods, for comparison.

386 The corrections (K) that PresRat requires to maintain the model-predicted precipitation
387 change are second order, arising from changes in the percentile at which the mean falls combined
388 with differing model-predicted changes at different percentiles, and so tend to be modest. Figure
389 4 shows K for four different months averaged across all 21 GCMs. In any given month Eq. 3
390 tends to alter the model-predicted mean change by less than 5% in the majority of the region
391 (white areas of Figure 4); in most other locations the mean is changed less than 20% (light and
392 dark green and yellow areas). In some places though, especially the dry regions of California in
393 summer, PresRat requires substantial corrections to preserve the model-predicted mean change.

394 By construction, PresRat preserves the model-predicted mean precipitation change
395 exactly in CCSM4 (bottom row of Figure 3). Although it is a minor effect, it is also worth noting
396 that PresRat allows the model to reproduce the observed historical mean in some cases where the
397 GCM has more zero-precipitation days than observed. In this situation the other bias-correction
398 techniques (QM, EDCDFm, and CDF-t) are unable to preserve the historical mean value since
399 there is no way to know which of the too numerous zero-precipitation model days should be

400 assigned a positive precipitation value (see section 3.1). This tends to be a minor effect because
401 in this situation it is the lowest precipitation days that the GCM is missing, and since
402 precipitation tends to have a strongly skewed distribution (especially in dry areas) the smallest
403 precipitation days contribute little to the monthly mean. Even PresRat cannot maintain the
404 model-predicted change if in the future period there is a month with no precipitating days to
405 correct, which does occur in some models for particularly dry locations and months.

406 PresRat generally preserves mean changes in precipitation while also allowing for
407 changes in the distribution. However a possible concern is that the multiplicative factor K is
408 calculated to preserve the GCM-predicted mean change but alters the bias-corrected future
409 values at all quantiles, not just the mean (i.e., PresRat does not preserve the model-predicted
410 ratio at each quantile after K is applied). The fact that K typically alters the values by less than
411 5% (Figure 4) should allay this concern to some degree but it is still worth checking explicitly.

412 An underlying uncertainty is that there is no straightforward approach for evaluating the
413 correctness of future distributions of climate variables. Using changes over the historical period
414 is possible but has the drawbacks noted in Maurer and Pierce (2013). As a practical matter we
415 compare future extreme precipitation values developed by PresRat to those from QM, CDF-t,
416 and EDCDFm. We cannot determine whether or not the distributions produced by PresRat are
417 correct just by comparing them with the distributions of other methods, but it is useful to know
418 how the methods compare.

419 Figure 5 shows how often each of the bias correction methods (QM, CDF-t, EDCDFm,
420 and PresRat) produces the smallest (rank 1) or largest (rank 4) 95th percentile value of future
421 (2070-99) winter (DJF) daily precipitation in each of the 21 global models. If the 4 bias
422 correction methods tended to produce equal values of the extrema, then on average each method

423 would produce 25% of the values in each rank. Accordingly the values shown in Figure 5 are the
424 difference (in percentage points) from 25%, so that positive values are seen where the bias
425 correction method is producing more values in that rank than the other methods by the end of the
426 century and negative values are seen where the method is producing fewer values of that rank
427 than the other methods. This highlights the dominance of any one method in contributing values
428 of a given rank. CDF-t and PresRat produce similar numbers of rank 1 (smallest) 95th percentile
429 values of future winter precipitation, while EDCDFm tends to produce considerably more rank 4
430 (largest) 95th percentile values than the other methods. PresRat has a surfeit of rank 2 (middle of
431 the pack) values compared to the other methods. While again emphasizing that we do not know
432 which of these representations is the most correct, we can nonetheless infer that an end-of-
433 century hydrological simulation using EDCDFm or QM bias corrected precipitation is likely to
434 produce more frequent or severe winter flooding events than one using PresRat. A similar
435 analysis for future summer (JJA) precipitation is shown in Figure 6; QM tends to show the
436 largest (rank 4) 95th percentile precipitation values and PresRat the smallest (rank 1) by the end
437 of this century. In other words, assuming that the model historical error at a given value is
438 preserved (as QM does) tends to lead to precipitation values that are more extreme than is
439 consistent with the factor that the GCM indicates the model precipitation will change by.

440 **3.6 Multi-model ensemble results**

441 Since bias correction affects different GCMs differently, it is useful to examine the effect
442 of bias correction on model-predicted changes aggregated across models. Figure 7 shows
443 projected changes (2070-99 relative to 1976-2005) in daily maximum temperature after bias
444 correction minus projected changes in the original GCM, averaged across all 21 GCMs. It is
445 apparent that QM and CDF-t have systematic effects, so an analysis of future temperatures

446 would not be protected against the tendency of these bias correction techniques to alter model-
447 predicted changes even if it used a relatively large ensemble of models. Some models show
448 alterations considerably larger than these mean values, so using a small number of models with
449 bias correction is potentially risky. QM, in particular, exaggerates model-predicted winter
450 warming across much of the north-central U.S. and diminishes summer warming through much
451 of the southeast. This provides justification for some implementations of QM (e.g., Wood et al.,
452 2004) to remove the GCM trend prior to bias correction and replace it afterward. As outlined in
453 Maurer and Pierce (2013), QM's modifications of the GCM trend are related to GCM
454 misrepresentations of variability in the historical model run. CDF-t shows much smaller mean
455 changes, but they still can exceed 0.5 °C in some locations. EDCDFm, by construction, shows
456 very little alteration of mean model-predicted changes in future daily maximum temperature.

457 Of course, when considering multi-model ensemble averaging the mean result might be
458 near zero but the individual models could have a large spread of values about zero. To determine
459 if this is the case, Figure 8 shows the RMS difference (calculated across the 21 GCMs) between
460 the original model-predicted future (2070-99) change in daily maximum temperature and the
461 change after bias correction has been applied. This largely confirms the interpretation of Figure
462 7; QM shows the greatest tendency to alter the original model-predicted changes in daily
463 maximum temperature, and CDF-t has both a reduced spread of results (compared to QM) and a
464 mean closer to zero. EDCDFm shows essentially no spread between models.

465 A similar analysis for future (2070-99) changes in daily precipitation is shown in Figure
466 9. In the multi-model ensemble average, QM, CDF-t, and EDCDFm all alter the mean GCM-
467 predicted future change in precipitation by more than 30 percentage points in some times and

468 locations, although generally CDF-t imposes smaller changes than QM and EDCDFm. QM has a
469 tendency to make the model-predicted changes wetter (cf. Maurer and Pierce 2013).

470 CDF-t tends to make forecast changes drier, for reasons that can be understood in terms
471 of Figure 1c. To produce a point on the bias corrected future distribution it is necessary that the
472 model historical value at the quantile being bias corrected fall within the range of observed
473 values, as indicated by vector (2) in Figure 1c. E.g., if vector (2) were progressively moved to the
474 right in Figure 1c, it can be seen that no historical values greater than $X=16$ mm/day (the
475 maximum observed value in Figure 1c) could be bias corrected. In this event, following
476 Michelangeli et al. 2009, the correction used is that found at the maximum valid historical value.
477 However the GCM precipitation simulations tend to display two attributes: 1) They over-predict
478 precipitation in dry areas, so the model CDFs are shifted to the right of the observed CDF (as
479 depicted in Figure 1c); 2) The most extreme precipitation events increase preferentially more
480 than others (e.g., IPCC 2007, 2013). In these situations CDF-t tends to be forced to use the
481 maximum valid correction, which falls at a lower quantile, and so misses the preferential
482 increase in the very highest quantiles. Figure 9 shows that this is only a modest tendency outside
483 of dry summer California/Great basin months, but could be a consideration for regional flooding
484 studies.

485 EDCDFm has mixed effects but makes the simulations strongly wetter in winter in the
486 Rocky Mountains and Great Basin, when much of those areas receive the bulk of their annual
487 precipitation, as well as the upper Midwest. In general EDCDFm will make predicted
488 precipitation changes wetter in locations where the GCM simulates a wetter climatology than
489 observed since a fixed model change (in the quantile) is being applied to a smaller historical base
490 value. By construction PresRat has little effect on the model-predicted mean change in future

491 precipitation, although the effect is not zero (in contrast to the results for EDCDFm with daily
492 maximum temperature) because a few of the models do not have enough precipitating days to be
493 corrected in certain months. This is particularly prevalent in California in July, where a number
494 of the GCMs have no July precipitation that can be altered by the bias-correction scheme. The
495 RMS spread of results across models (Figure 10) shows roughly comparable values for QM and
496 EDCDFm and nearly as much for CDF-t, while PresRat has much less spread. As found in the
497 mean results, the locations where PresRat does show model spread is due to occasional models
498 predicting too little precipitation in some month for a correction to be applied.

499 **3.7 Summary: preserving model-predicted mean changes**

500 The QM and CDF-t bias correction methods generally alter model-predicted mean
501 changes in daily maximum temperature and precipitation. EDCDFm, however, effectively
502 preserves model-predicted changes in mean daily maximum temperature. PresRat (which is a
503 new extension of EDCDFm to preserve ratios, add a zero-precipitation threshold, and implement
504 a correction factor) preserves model-predicted future changes in precipitation (evaluated as a
505 ratio) as long as there exist precipitating days in the GCM simulation that can be corrected. This
506 is accomplished with only modest correction factors (generally less than 5%, the notable
507 exception being the very dry California summers). The extreme values produced by PresRat are
508 mostly consistent with the extreme values from the other bias correction methods, though it tends
509 to produce fewer of the highest 95th percentile values than EDCDFm (in winter) or QM (in
510 summer).

511 In summary, both temperature and precipitation can be bias corrected using methods that
512 preserve global climate model-predicted future mean changes. Doing so would help minimize
513 confusion and inconsistent results between downscaled regional climate simulations and global

514 model analyses, such as represented by the IPCC analyses (2007, 2013). The advantage of this
515 approach over that taken in Wood et al. (2002), where the trend is removed, bias correction
516 performed, and the interpolated trend re-introduced, is that the model-predicted changes
517 themselves can be downscaled rather than being only interpolated GCM fields.

518 **4. Frequency Dependent Bias Correction**

519 **4.1 Overview**

520 The previous section examined the effect of bias correction on GCM-predicted mean
521 changes at long time scales (decades). In this section we address more general question of what
522 model biases may be present across the gamut of timescales and how to address them. Quantile-
523 based bias correction methods such as QM, EDCDFm, CDF-t, and PresRat already alter the
524 variance spectrum of the GCM's time series if certain quantile values do not appear at random
525 intervals in the time series, but rather preferentially at certain frequencies. For example the
526 highest quantiles of California precipitation generally appear in winter, so the proportion of
527 variance in the annual cycle will typically be altered by bias correction. However this effect is
528 modest, as will be shown quantitatively below.

529 The frequency-dependent bias correction method developed here is designed to
530 systematically alter the shape of the GCM's spectrum to better match observations without
531 changing the overall variance. As such, it is intended to be applied as an additional processing
532 step after standard bias correction has already adjusted the overall variance.

533 Details are given in the following sections, but in broad terms, the frequency dependent
534 bias correction proceeds as follows. First, the variance spectra of the observations and model are
535 calculated. The model variance error as a function of frequency is then computed as the ratio of

536 the spectral values, (model/observed). To correct these errors the model time series is Fourier
537 transformed to frequency space, then the amplitude of the Fourier components are adjusted so
538 that the distribution of variance across frequencies better matches observations. The Fourier
539 components are then inverse transformed back into a time series.

540 Much of the following material is devoted to examining the result to make sure the
541 process improves the model simulation rather than degrading it. However, one caveat is that the
542 spectral approach used here does not consider frequency-dependent biases in different seasons or
543 months, but instead only as a collective whole over the entire time period. This potentially means
544 that it is not feasible to expect a removal of biases across all timescales of interest by this
545 technique.

546 **4.2 Spectral Methodology**

547 Since we bias correct the future model projections in 30-yr periods (section 2.3), the
548 PresRat method outlined in section 3.4 will preserve model-predicted mean changes at periods of
549 30 years and longer in the future projection. Accordingly, when we consider frequency-
550 dependent bias corrections we need only include, at most, periods from two days (the Nyquist
551 frequency given the daily model output) to 30 years. This interval will be further refined below
552 in light of our spectral analysis technique. Model predicted changes at these frequencies can arise
553 from natural internal climate variability, anthropogenic causes, or both.

554 Numerous techniques are available to compute variance spectra (for a review, see Ghil et
555 al. 2002). Many of the newer methods have been developed to identify narrow-band signals
556 against a background of noise. However, in this work we are also concerned with the power in
557 the broad parts of the spectrum that might in other applications be considered simply “noise”.
558 This variability represents weather and climate fluctuations that affect hydrology and ecosystems

559 across a wide range of time scales, so we seek as realistic a simulation of these fluctuations as
560 possible. Accordingly we use relatively wide bandwidths in this work and employ the Jenkins
561 and Watts (1969) method of computing variance spectra as the Fourier transformation of the
562 autocovariance function. We require at least 40 degrees of freedom in the spectral estimates,
563 which given 30 years of daily data and a Parzen lag window, means truncating the
564 autocovariance function after 1020 lags (Jenkins and Watts 1969). Following the Jenkins and
565 Watts recommendations the number of frequencies is set to twice the number of lags (2040), so
566 the first non-zero frequency corresponds to a period of ~11 yrs. Longer periods are unresolved,
567 and the frequency-dependent bias correction does not alter their relative proportion of variance.

568 With over 2000 frequencies spanning from 2 days to 11 years it is useful to reduce the
569 number of frequencies at which the model error is corrected to avoid spurious over-fitting.
570 Accordingly, the frequency-dependent model errors are calculated in a reduced set of 100
571 frequency bins of equal width in the logarithm of frequency. This means that higher frequency
572 bins have multiple samples, as shown in Figure 11, with more than 5 samples per bin at periods
573 shorter than ~80 days (purple lines). The binning therefore reduces the uncertainty in the spectral
574 estimates for periods shorter than ~80 days. The average value of the spectrum in a bin is
575 estimated using monotonic cubic splines (Fritch and Carlson 1980) to avoid abrupt changes in
576 the estimate depending on whether a frequency point is barely included or excluded from a bin.

577 Von Storch and Zwiers (2001) note the problems in interpreting spectral plots on a
578 logarithmic frequency axis, since the displayed area under the spectrum is no longer proportional
579 to the variance. It is possible to maintain the property of being a spectral density if the spectral
580 value is multiplied by frequency, or if the plotted values are integrated (as opposed to averaged)
581 across constant widths of the logarithmic frequency axis. However these approaches change the

582 angle of a plotted spectrum (for example, a white spectrum is then no longer flat), which can be
583 confusing. To avoid this potentially misleading situation, values shown here are simply averaged
584 in frequency so that the spectra appear similar to what is typically found in the literature (i.e., a
585 white spectrum is flat).

586 **4.3 Frequency dependent model errors**

587 Figure 12 shows maps of the observed (1976-2005) distribution of variance in daily
588 maximum temperature across frequencies (labeled using equivalent periods) and the multi-model
589 ensemble errors in representing this distribution in the same period. The left column shows
590 observations (% of total variance), the middle column shows the multi-model mean error (%)
591 with respect to the observations, and the right hand column shows multi-model RMSE (%; i.e., at
592 each point, the spread of values across the 21 models). The frequency-dependent bias correction
593 is based on normalized spectra (spectral values divided by the variance of the original time
594 series) so that it leaves the overall variance unaltered. Therefore at every location the values in
595 the left hand column summed across frequency bands total 100%. For example, the top left panel
596 of Figure 12 shows that in the region from western Texas north to western Kansas more than
597 10% of the total variance falls in the 2-10 day band, while in the region immediately to the west
598 less than 4% does.

599 As expected, Figure 12 shows that the annual cycle dominates the daily maximum
600 temperature variability over almost all of the conterminous U.S., containing on average 62% of
601 the total variance. The exception is in locations along the California coast, where shorter period
602 variability makes a much larger contribution to the overall variance than found elsewhere.

603 Reinforcing the notion that bias correction might usefully be applied as a function of
604 frequency, the multi-model aggregate profile of model errors of daily maximum temperature

605 (middle column) varies considerably across the spectral range. Over much of the domain there is
606 a tendency for models, on average, to allocate less of the total variance to periods shorter than 3
607 months than is observed, particularly in the 10-30 day band where the mean error is -9%. RMS
608 errors at periods shorter than the annual cycle are typically on the order of 10-15% of observed
609 variance in those frequency bands, which implies that the mean error is relatively consistent
610 across the models. The proportion of variance in the annual cycle is represented with virtually no
611 mean error and a very small spread across models.

612 A deficiency in daily maximum temperature variability at periods shorter than the annual
613 cycle combined with an accurate representation of the annual cycle implies that periods longer
614 than the annual cycle must be receiving proportionally too much variance, which is confirmed by
615 Figure 12b. Variability that occurs at periods longer than 30 months has, on average,
616 proportionately ~40% more variance than observed, and the spread across models is large, with
617 RMS errors of ~60%. However it should be kept in mind that the fraction of total variance
618 contained in these long time scales is quite small ($< 1\%$ for all timescales longer than 30
619 months).

620 Figure 13 shows the same frequency-dependent analysis using daily precipitation. In
621 contrast to daily maximum temperature, over most of the conterminous U.S. the shortest periods
622 (2-10 days) contain the majority of the variance (on average, 62%). The exception is the wet
623 parts of the west coast, where 10-30 day and longer period variability is nearly as important and
624 the annual cycle contains $> 7\%$ of the total variance, more than twice the average at that
625 frequency over the domain. The models as a group tend to simulate the short-period (2-10 day)
626 fraction of total variance reasonably well, with a modest (5-10%) mean bias towards too much
627 short-period variability along the west coast and upper Midwest and too little around Texas,

628 Oklahoma, and the Gulf coast. Figure 13b shows that model-simulated precipitation variability at
629 periods of 30 months or longer accounts for an anomalously large proportion of the total
630 variance in the southeastern U.S., and an anomalously small proportion in the Pacific Northwest.
631 Rupp et al., (2013) also found that models overestimate temperature variance at timescales
632 longer than a year and underestimate precipitation variance at timescales longer than a year in
633 the Pacific Northwest, USA. Disagreements across the models are large at these longer periods.

634 **4.4 Correcting frequency-dependent model errors**

635 *4.4.1 Method for frequency-dependent bias correction*

636 To correct the frequency-dependent model biases at some location, the ratio σ of the
637 model's variance spectrum to the observed variance spectrum is computed in each of the 100
638 logarithmically spaced frequency bins. This step is analogous to calculating the ratio of model to
639 observed values at each quantile in the cumulative distribution function in the PresRat method.
640 Both spectra are computed over the historical climatology period, 1976-2005. The original model
641 time series is then transformed to frequency space and, to bias correct the model series, the
642 amplitude of the Fourier components are multiplied by $\sigma(f)^{-1/2}$ (the square root accounts for
643 the fact that variance is proportional to the amplitude of the Fourier components squared). The
644 result is then transformed back to the time domain. As typical in statistical bias correction
645 techniques, σ is calculated over the control period and applied to both the control and future
646 periods. This assumes that the statistics of the model error as a function of frequency do not
647 change, but does not prevent a model from changing its future spectrum, either the overall
648 amplitude of variance or the distribution of variance across frequencies; it just means that any
649 model-predicted changes will be relative to the corrected model spectrum.

650 *4.4.2 Example results for daily maximum temperature*

651 As noted above, standard bias correction techniques such as QM, EDCDFm, and CDF-t
652 alter the spectra of the time series they are applied to. Thus, in order to clearly demonstrate the
653 effect of the frequency-dependent bias correction by itself, we first present results using only the
654 frequency-dependent bias correction. We then show combined results using the frequency-
655 dependent bias correction applied in conjunction with standard bias correction.

656 Typical results of the frequency-dependent bias correction using daily maximum
657 temperature from the CCSM4 GCM are illustrated in Figure 14. The left column shows
658 normalized spectra of observations (red), the original model (blue), and the model after
659 frequency-dependent bias correction (green dots). For each panel values are taken from the
660 location indicated by the purple ‘x’ on the inset map and shown in the panel’s title (longitude,
661 latitude). The right column shows the ratio of the model’s spectral value to the observed value,
662 both before (blue) and after (green dots) the frequency-dependent bias correction is applied.

663 It is useful to define a root mean squared error metric appropriate for ratios of the spectral
664 values, which we designate as log-RMSE to differentiate it from standard RMSE measures that
665 are appropriate to differences rather than ratios. Let $\epsilon = \ln \sigma$, then

$$\text{log-RMSE} \equiv \exp(\sqrt{\langle \epsilon^2 \rangle}) - 1 \quad (5)$$

666 where the angle brackets indicate the mean over the logarithmically spaced frequency values.

667 This expression treats equal ratios of error equally (i.e., the model having twice the observed
668 variance produces the same error as the observations having twice the model’s variance), and the
669 final -1 makes a perfect result (model variance equal observed, so $\sigma = 1$) give a log-RMSE of 0.

670 In general, if the model values are incorrect (on average across log-spaced frequencies) by a

671 factor of σ then the log-RMSE is $\sigma - 1$. These log-RMSE values are indicated in the right column

672 of Figure 14. When we refer to log-RMSE below, we specifically mean the model's error in
673 reproducing the distribution of variance across frequencies, as illustrated in Figure 14.

674 In some locations, such as the San Francisco region (top row of Figure 14), the ratio of
675 the model variance to observed exhibits a notable slope (top right panel) which indicates that the
676 model frequency errors are a systematic displacement of variance, depriving high frequencies
677 and enriching low frequencies. At all locations the frequency-dependent bias correction improves
678 the model's representation of how variance is distributed across frequencies. The log-RMSE
679 typically drops by about a factor of 5 as a result of the correction. Some residual error remains
680 due to the approximate nature of corrections calculated using discretely sampled data on a finite
681 interval.

682 *4.4.3 Example results for daily precipitation*

683 Precipitation is more difficult to correct than temperature because it cannot have negative
684 values, which limits the adjustments that the frequency-dependent bias correction can produce.
685 There are also many days with zero precipitation, which we do not alter. In fact, to avoid
686 potential problems with exacerbating models' drizzle problem, whereby they produce too many
687 days of light precipitation (Sun et al. 2006; Dai 2006), we leave unmodified any model
688 precipitation values less than 1 mm/day. Particularly in dry areas this can leave few days for the
689 frequency-dependent bias correction to operate upon.

690 Precipitation results at a few example locations are shown in Figure 15 using CCSM4. It
691 is apparent that the frequency dependent bias correction is less effective at adjusting precipitation
692 than temperature. For example log-RMSE values only decrease by a factor of 1.3 to 2 rather than
693 a factor of 5, as found for temperature. But although the corrections are relatively modest, they
694 result, uniformly, in the direction of decreasing model error and so are helpful.

695 *4.4.4 Multi-model ensemble average results*

696 The multi-model ensemble average log-RMSE for daily maximum temperature is shown
697 in the top row of Figure 16 both before (left column) and after (middle column) the frequency-
698 dependent bias correction. The models systematically disagree with the observations, particularly
699 along the west coast and in a band extending north from northern Texas. Before the frequency-
700 dependent bias correction the mean log-RMSE of daily maximum temperature error of 0.50
701 indicates that the models are, on average across models, locations, and frequencies, off by a
702 factor of 1.50 (i.e., by 50%) in their representation of the variance in any particular frequency
703 band. After frequency-dependent bias correction the log-RMSE drops to 0.11 (nearly a factor of
704 five decrease), indicating that the corrected models are only off by a factor of 1.11 on average.

705 Results for daily precipitation are shown in the bottom row of Figure 16. The models as a
706 group tend to do worse in the Rocky Mountains and Great Basin than in most other locations.
707 The mean log-RMSE for precipitation is approximately the same as for daily maximum
708 temperature. However, as expected for the reasons given above, precipitation is less easily
709 corrected than temperature; the log-RMSE for precipitation drops by less than a factor of 2 after
710 the frequency-dependent bias correction. The pattern of log-RMSE precipitation errors after
711 correction (Figure 16, lower center) primarily reflects the rate of occurrence of days with > 1
712 mm/day of precipitation (our threshold for correction). The final results are best where the most
713 potentially correctable precipitation values exist and worst where there are few correctable days.
714 However this does not completely explain the pattern; there are residual differences that reflect
715 the seasonality and other aspects of the local precipitation distribution.

716 An important consideration is whether the frequency-dependent bias correction makes the
717 representation of variance with frequency worse in some locations despite being better on

718 average. This is addressed by the histograms in Figure 16 (right column), which show the
719 difference between each location's corrected and original log-RMSE, pooled across every
720 location and every model. On average the frequency-dependent bias correction decreases the log-
721 RMSE for daily maximum temperature by 0.39, and this is accomplished without making any
722 locations worse (no positive values are seen in the histogram). Even for precipitation, which
723 shows less improvement (decrease of log-RMSE by 0.21) from the frequency-dependent bias
724 correction than temperature, the correction virtually always decreases the log-RMSE (lower right
725 panel of Figure 16).

726 *4.4.5 Magnitude of the corrections*

727 It would be potentially troubling if the modifications to the time series made by the
728 frequency-dependent bias correction were too large. Histograms of the amplitude of the
729 corrections pooled across all models and locations are shown in Figure 17. Any day's maximum
730 temperature is changed less than 3°C about 95% of the time, although rarely the changes can
731 exceed 4°C. The change in precipitation is less than 40% or 1.5 mm day⁻¹ about 95% of the time,
732 although on rare occasion can be more than 50% or 2.5 mm day⁻¹. Since the frequency-
733 dependent bias correction operates on normalized spectra, altering the distribution of variance
734 across frequencies without altering the overall variance, the mean changes are approximately
735 zero for both temperature and precipitation.

736 Time series of daily maximum temperature before and after the frequency-dependent bias
737 correction are shown in Figure 18, using year 2000 from the CCSM4 GCM as an example. For
738 plotting purposes the annual mean value (shown in the upper right part of the panel) has been
739 removed. The changes to the time series made by the frequency-dependent bias correction are
740 small compared to the synoptic and annual timescale fluctuations in the time series. Similar time

741 series for daily precipitation are shown in Figure 19. Again, the modifications made by the
742 frequency-dependent bias correction are modest compared to the daily variability. The relatively
743 constrained nature of the changes imposed by the frequency-dependent bias correction shows
744 that the improvement in spectral properties afforded by the frequency-dependent bias correction
745 does not come at the expense of creating an unrealistic time evolution in the final fields.

746 *4.4.6 Combined effects of standard and frequency-dependent bias correction*

747 In this section we explore the effect of frequency-dependent bias correction applied in
748 conjunction with standard bias correction. Only the historical period is considered since we
749 compare to observations. This in turn restricts this analysis to QM since the other bias correction
750 methods differ from QM exclusively in the future period.

751 Figure 20 shows the multi-model mean log-RMSE across all the climate models for daily
752 maximum temperature, both before any bias correction has been applied (panel a) and after
753 various combinations of QM and frequency-dependent bias correction have been applied (panels
754 b-e). QM by itself decreases the mean log-RMSE by about 0.15, compared to the frequency-
755 dependent bias correction, which decreases the mean log-RMSE by about 0.39. So although QM
756 helps make the models' distribution of variance across frequencies closer to observed, the
757 improvement is considerably smaller than that achieved by the frequency-dependent bias
758 correction. Panels d and e show the results when applying the frequency-dependent bias
759 correction either before or after QM. On average results are slightly better when the frequency-
760 dependent bias correction is applied after QM, although the difference is small.

761 Figure 21 shows the same analysis for daily precipitation. QM does a slightly poorer job
762 of improving the models' depiction of variance across frequency than seen when operating on
763 daily maximum temperature (a reduction in log-RMSE of 0.12 for precipitation vs. 0.15 for

764 temperature). However, as noted above, the frequency-dependent bias correction is not as
765 effective in correcting precipitation as temperature (log-RMSE drops by 0.21 for precipitation vs.
766 0.39 for temperature), although it still provides almost twice the reduction in log-RMSE than
767 found in QM alone (0.21 vs. 0.12). As found for daily maximum temperature, slightly better
768 results are obtained when QM is followed by the frequency-dependent bias correction rather than
769 the opposite order.

770 It was previously noted (Figure 16) that one desirable aspect of the frequency-dependent
771 bias correction is that no location's agreement with observations becomes worse as a result of the
772 method being applied. Figure 22 shows a similar analysis for daily maximum temperature (top
773 row) and precipitation (bottom row) using various combinations of QM and frequency-
774 dependent bias correction. QM degrades the agreement between the model and observations in
775 how variance is distributed across frequencies at about 9.6% of the locations (pooled across all
776 models) for temperature and 23% for precipitation. Of course QM was not designed to take into
777 account the variance spectrum of the simulation so this is not a surprising result, but it is
778 nonetheless worth pointing out this previously unidentified drawback of QM. When frequency-
779 dependent bias correction is followed by QM (bottom right panel), 4.5% of the precipitation
780 locations show worse agreement with observations than the original model even though the mean
781 result is to improve the agreement. However when the order of operations is reversed, so that
782 QM is followed by frequency-dependent bias correction, only 1.3% of the precipitation locations
783 show a worse agreement with observations than found in the original model and no locations
784 show a worse agreement for daily maximum temperature. These findings, along with the results
785 from Figure 20 and Figure 21 that show a small but consistent superiority when applying QM

786 before the frequency-dependent bias correction, are the reason we perform the operations in this
787 order.

788 Although these results show that it is better to apply the frequency-dependent bias
789 correction after QM, a point of concern is what effect this might have on the quantile matching
790 bias correction that QM performs. Does the frequency-dependent bias correction significantly
791 degrade the correspondence between modeled and observed quantiles that QM imposes? This is
792 evaluated in Figure 23, which shows quantile-quantile plots comparing the quantile at which a
793 value falls in the observed distribution to the quantile at which the same value falls in the
794 models' distributions. Plotted values are pooled across all models and locations. If the models
795 had a perfect representation of the observed distribution, then all the model values would fall
796 along a straight line with slope of 1 (dashed green line in Figure 23). The box and whiskers in the
797 figure show the distribution of model values that are found for a given observed quantile. For
798 example, the upper left panel of Figure 23 shows that the median (0.50 quantile) observed value
799 of daily maximum temperature is, in the median, found at the 0.55 quantile in the models, so the
800 models as a group have a slight cold bias relative to the observations. Half the time the observed
801 median value is found between the 0.50 and 0.60 quantile in the models; and 90% of the time the
802 observed median value is found between the 0.45 and 0.70 quantile in the model. 5% of the time
803 the observed median value falls either below the 0.45 quantile or above the 0.70 quantile in the
804 model.

805 Figure 23 shows that, viewed across their CDFs, the models do better simulating the
806 distribution of daily maximum temperature than precipitation; at least 25% of the models
807 simulate the observed quantile of daily maximum temperature correctly, no matter what
808 observed quantile is considered. For precipitation however, notably less than 25% of the models

809 manage to simulate the observed percentile correctly at quantiles < 0.5 , and at the lowest quantile
810 plotted less than 5% of the models are able to simulate the observed percentile. The positive
811 precipitation bias at low quantiles is consistent with the models' drizzle problem.

812 For our purposes, the left two columns of Figure 23 shows that the frequency-dependent
813 bias correction does not systematically alter the shape of the model distributions, which is by
814 design since the method is intended to leave the overall variance unchanged. When QM is
815 applied, either before frequency-dependent bias correction or after (right two columns of Figure
816 23), the agreement between observed and modeled quantiles is quite good. This is an outcome of
817 QM by construction, and the frequency-dependent bias correction changes that result only a
818 little.

819 Overall we conclude that the frequency-dependent bias correction does not inflict
820 additional problems to the resultant adjusted model output. Furthermore, it is useful to apply
821 since it increases the average agreement between the observed and modeled distribution of
822 variance across frequencies without degrading the agreement at any location. It accomplishes
823 this with relatively small and symmetric corrections (typically $< 3^{\circ}\text{C}$ or 2 mm/day) without
824 imposing spurious behavior in time or diminishing the agreement between modeled and observed
825 quantiles that QM imposes.

826 **5. Summary and Conclusions**

827 GCMs generally produce biased simulations of variables such as temperature and
828 precipitation. It is necessary to remove these biases before using the model-simulated fields in
829 applications that have non-linear sensitivities to biases, such as land surface or hydrological

830 modeling. Accordingly, a bias correction step is often performed on GCM fields before use in
831 such applications.

832 One problem with bias correction methods such as quantile mapping (QM; e.g., Wood et
833 al. 2002) and the CDF-transform method (CDF-t; Michelangeli et al. 2009) is that they alter
834 GCM-predicted mean future changes, evaluated here as 2070-99 relative to 1976-2005.
835 Compared to the original changes produced by an ensemble of 21 GCMs with the RCP 8.5
836 anthropogenic greenhouse gas and aerosol scenario, QM produced warmer future daily
837 maximum temperatures by up to 2°C across much of the upper Midwest, California coast, and
838 Northern Rockies in January, and cooler daily maximum temperatures by up to 2°C across much
839 of the southeastern part of the U.S. in July. CDF-t showed smaller alterations of up to 0.5°C, but
840 they may still have consequence because they tend to persist throughout the year. When
841 evaluated as a multiplicative change in precipitation, QM and the equidistant CDF matching
842 method (EDCDFm; Li et al. 2010) produced wetter conditions than projected by the original
843 global models by up to 30 percentage points across the upper Midwest and Northern Rockies in
844 January, while CDF-t produced drier conditions by up to 20 percentage points in the Southwest
845 U.S. in summer. These changes are large enough to make a practical difference in the results of
846 climate impact studies, which is problematic given their widespread usage and because the
847 magnitude of changes imposed through bias correction can be of the same order of magnitude as
848 the model predicted changes by the end of the century. Moreover, because analyses of the
849 projected climate changes in the original GCMs are widespread (e.g., IPCC 2007, 2013),
850 alterations to the GCM trends may lead to inconsistencies and confusion in bias-corrected
851 regional studies.

852 In the first part of this work we have demonstrated a methodology that uses existing and
853 modified techniques to maintain model-projected climate changes even when bias correcting the
854 global model data.

855 Under the assumption that bias correction should preserve the model projected future
856 change, EDCDFm works very well for temperature projections. For precipitation projections we
857 have introduced an extension to EDCDFm that we term PresRat, which “preserves the ratio” of
858 future changes rather than the difference, includes a zero-precipitation threshold that makes the
859 modeled number of zero-precipitation days match observations, and adds a correction factor that
860 is typically $< 5\%$. PresRat generally maintains model-predicted changes in daily precipitation.
861 However none of the bias correction techniques, PresRat included, can preserve the model-
862 predicted precipitation change in cases where locations that are so dry there are insufficient
863 precipitation days to bias correct (which is rare, but does happen in some models during the dry
864 months).

865 In the second part of the study we extend our examination of model biases from trends to
866 the more general issue of the models’ representation of variance across a range of timescales, and
867 introduce a frequency-dependent bias correction method that can address inaccuracies in the
868 GCM simulations. A comparison with observations showed that as a group, the 21 GCMs
869 apportion too little variability of daily maximum temperature to times scales between 10 and 90
870 days and too much to time scales longer than 30 months. The models’ simulation of daily
871 precipitation variability was more mixed, but at long timescales (> 30 months) they show more
872 variability than observed in the Gulf coast region and less than observed in the Pacific
873 Northwest.

874 We showed that the models' simulation of variance as a function of frequency can be
875 improved by a frequency-dependent bias correction, which is implemented as digital filter in the
876 frequency domain. Before the frequency-dependent bias correction the model simulations tend to
877 err in their estimate of the frequency distribution of total daily maximum temperature variance
878 by a factor about 1.5, RMS averaged across log-spaced frequencies. After the frequency-
879 dependent bias correction the RMS error drops to a factor of 1.11. Precipitation cannot be
880 corrected as easily as temperature since locations typically have numerous zero-precipitation
881 days, but the frequency dependent bias correction stills decreases the RMS error from a factor of
882 1.49 to 1.28. These improvements are accomplished with relatively modest alterations to the
883 original values, typically $< 3^{\circ}\text{C}$ in daily maximum temperature and < 1.5 mm/day in daily
884 precipitation.

885 The frequency-dependent bias correction improves the models' simulation of variance as
886 a function of frequency about twice as much as standard bias correction. Additionally the
887 frequency-dependent bias correction makes no locations worse, while standard bias correction
888 degrades the simulated distribution of variance across frequencies at about 9.6% of the gridpoints
889 (pooled across all 21 global models) for daily maximum temperature and 23% for precipitation.
890 Applying the frequency-dependent bias correction subsequent to standard bias correction both
891 increases the models' mean agreement with observations substantially (better than either
892 technique applied alone) and reduces the fraction of degraded gridpoints to 0.0% for daily
893 maximum temperature and 1.3% for precipitation.

894 Important questions about bias correction remain. This study has not addressed whether
895 bias correction *should* be applied at any particular location given that model-observational
896 disagreements are influenced by natural climate variability, which can be large and affect climate

897 means over years to decades (e.g., Maraun et al. 2010; Deser et al. 2012). Likewise, it is not clear
898 if models should be bias corrected to a particular period that tree ring or other paleoclimate
899 evidence suggests is atypical. Although these are interesting questions, in this work we have
900 followed the common practice of applying bias correction to the GCMs at all locations to bring
901 them into agreement with a pre-selected recent climatological period.

902 Another problem with bias correction techniques that is not addressed here is that a
903 model with a seasonal cycle of precipitation that is greatly different from observations might not
904 preserve the GCM-predicted annual change even if all precipitation trends are preserved at the
905 monthly time scale. This reinforces the fact that although bias correction can help make the
906 statistics of temperature and precipitation fields from a global climate simulation more like
907 observations, it is possible for some models in some regions to produce such a poor simulation
908 that bias correction has little meaning. Even before bias correction care should be taken to ensure
909 that GCMs used in a regional climate impact study capture the relevant physical processes to
910 begin with. For example, a GCM that lacks an ENSO cycle or seasonal monsoon flow can be
911 bias corrected and downscaled like any other model, but the result will have little meaning in
912 areas that are influenced by ENSO or monsoonal flow.

913 In the end, as global climate model results continue to be applied to investigate
914 phenomena that are sensitive to model biases, bias correction will become an ever more
915 important step. The bias correction methods outlined here can improve these simulations, giving
916 a clearer picture of future climate conditions for a variety of applications.

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923 <http://gdo-dcp.ucllnl.org>.

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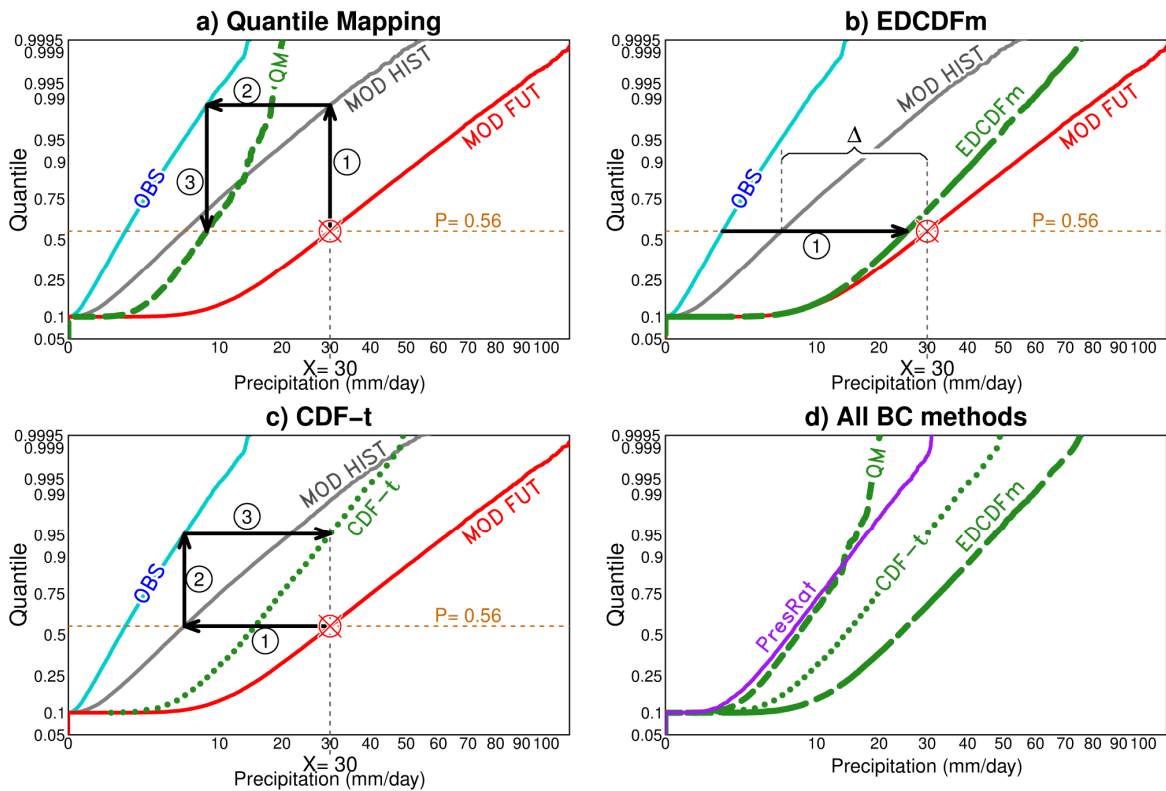
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Abbreviation	Model source/institution
Access1-0	Commonwealth Scientific and Industrial Research Organization (CSIRO) and Bureau of Meteorology (BOM), Australia
Bcc-csm1-1	Beijing Climate Center, China
Bnu-esm	Beijing Normal University, China
CanESM2	Canadian Centre for Climate Modelling and Analysis, Canada
CCSM4	National Center for Atmospheric Research, USA
ECSM1-BGC	National Center for Atmospheric Research, USA
CNRM-CM5	Centre National de Recherches Meteorologiques, France
CSIRO-Mk3.6.0	QCCCE & Commonwealth Scientific and Industrial Research Organization, Australia
GFDL-CM3	Geophysical Fluid Dynamics Laboratory, Princeton, USA
GFDL-ESM2G	Geophysical Fluid Dynamics Laboratory, Princeton, USA
GFDL-ESM2M	Geophysical Fluid Dynamics Laboratory, Princeton, USA
INMCM4	Institute of Numerical Mathematics Russian Academy of Sciences, Russia
IPSL-CM5a-LR	Institut Pierre-Simon Laplace, France
IPSL-CM5a-MR	Institut Pierre-Simon Laplace, France
MIROC-ESM	Japan Agency for Marine-Earth Science and Technology, and National Inst. For Environ. Studies, Japan
MIROC-ESM-CHEM	Japan Agency for Marine-Earth Science and Technology, and National Inst. For Environ. Studies, Japan
MIROC5	Atmosphere and Ocean Research Institute and Nat. Inst. For Environ. Studies, Japan
MPI-ESM-LR	Max Planck Institute for Meteorology, Germany
MPI-ESM-MR	Max Planck Institute for Meteorology, Germany
MRI-CGCM3	Meteorological Research Institute, Japan
NorESM1-m	Norwegian Climate Centre

Table 1. The GCMs used in this work and their originating institutions.



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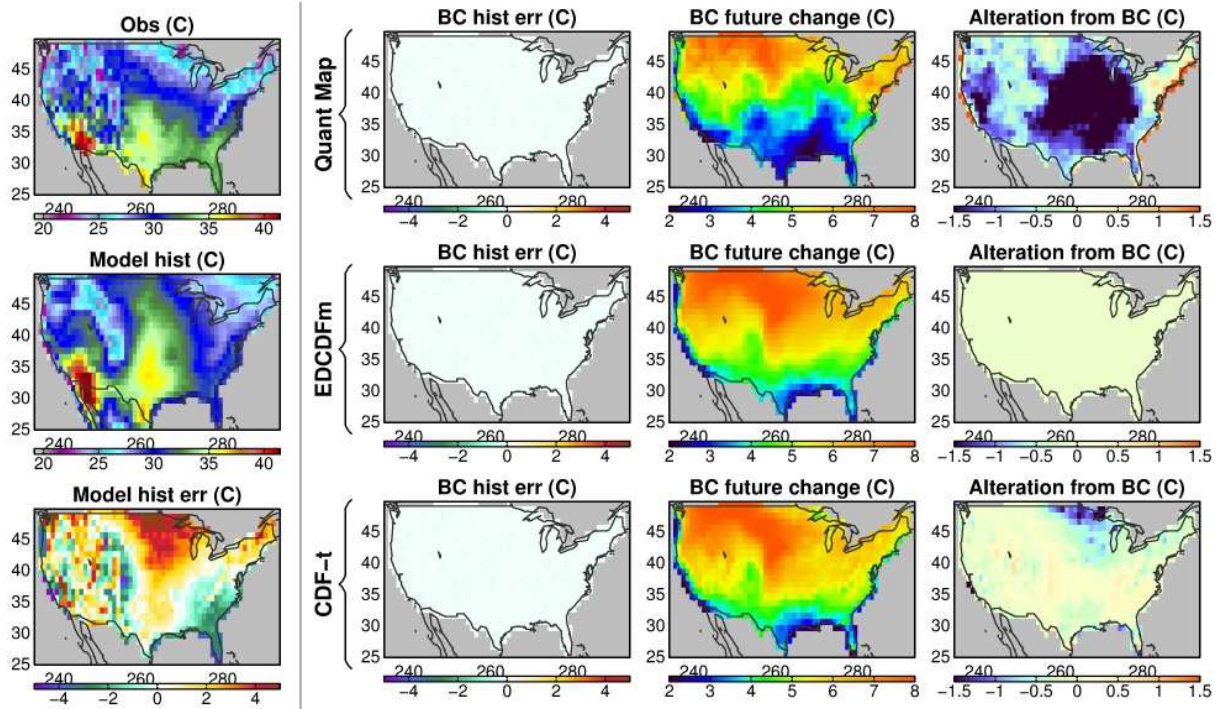
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Figure 1. Cumulative distribution functions (CDFs) of synthetic daily precipitation data schematically illustrating how each bias correction method constructs the model's bias corrected future CDF (green dotted/dashed lines). The solid blue, grey, and red lines are the same in all panels and show the observed (1976-2005), model historical (1976-2005), and model future (2070-2099) CDFs, respectively. The example point being corrected is $X=30$ mm/day, which falls at the 0.56 quantile in the model future distribution (dotted orange line). a) Quantile mapping (QM): starting at the point to be corrected, go vertically to the grey line (1), horizontally to the blue line (2), and vertically to the original percentile (3). b) Equidistant CDF matching (EDCDFm): at the quantile of the point being corrected, compute the offset from the model historical value to the model future value (Δ), then add Δ to the observed value at the percentile being corrected (1). c) The CDF-transform (CDF-t) method; starting at the point to be corrected, go horizontally to the grey line (1), vertically to the blue line (2), and horizontally to the original value (3). d) Final results from all 3 bias correction methods (dotted/dashed green lines), along with the PresRat method (solid purple line) for comparison. Note that the X axis uses a square root transformation and the Y axis uses an inverse error function ("probability plot") transformation.



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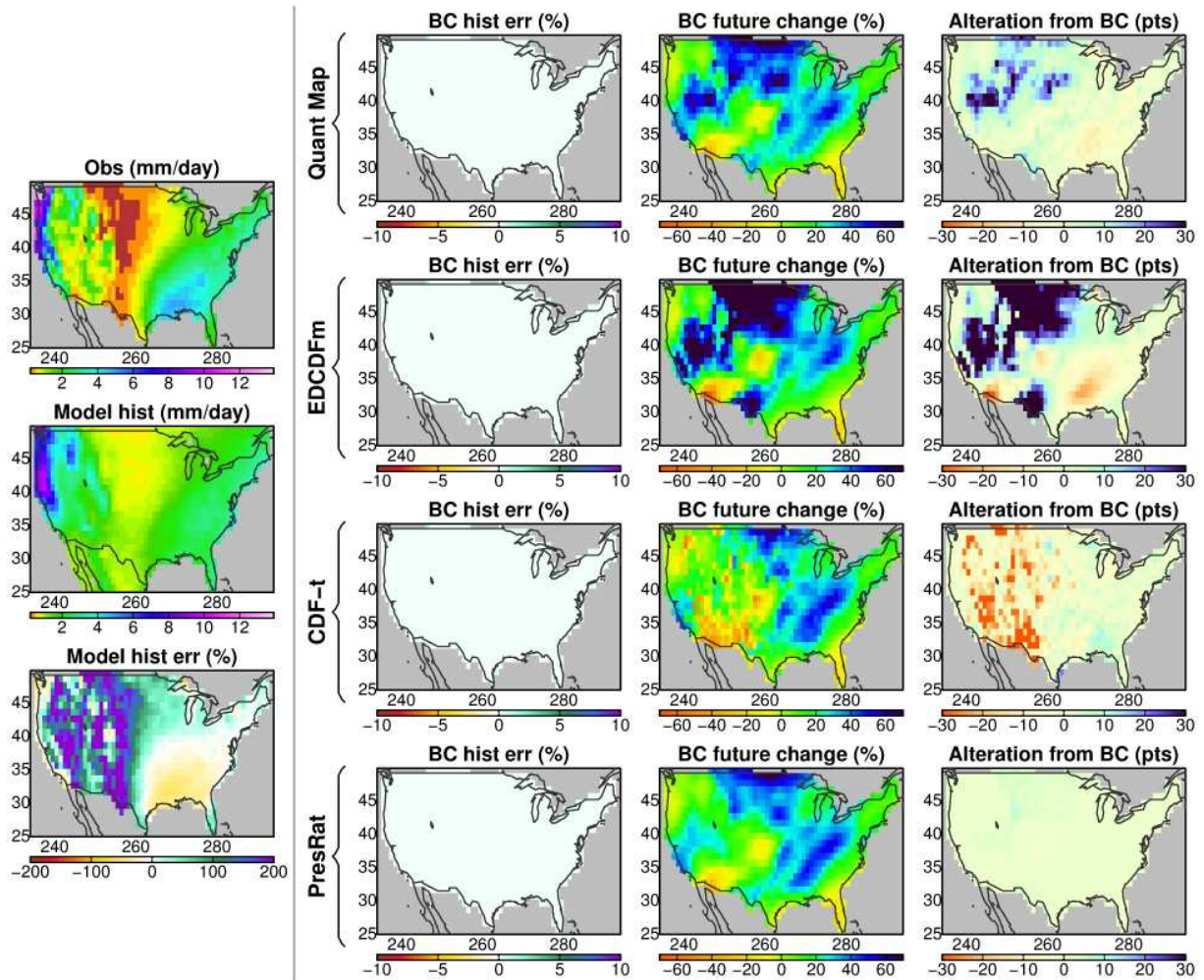
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Figure 2. Illustration of how bias correction can alter the model-predicted future change in monthly-averaged maximum daily temperature, shown for July using the CCSM4 GCM. Left column: the observations, model simulation over the historical period (1976-2005; °C), and model error with respect to observations without any bias correction (°C). Right part of figure: For each of the bias correction methods indicated (quantile mapping (upper row), EDCDFm (middle row), and CDF-t (lower row)) shown are the model error with respect to observations over the historical period after bias correction has been applied (°C), the model-projected future change (2070-2099) after bias correction using the indicated method (°C), and the amount that the bias correction method alters the original model-predicted change (°C).

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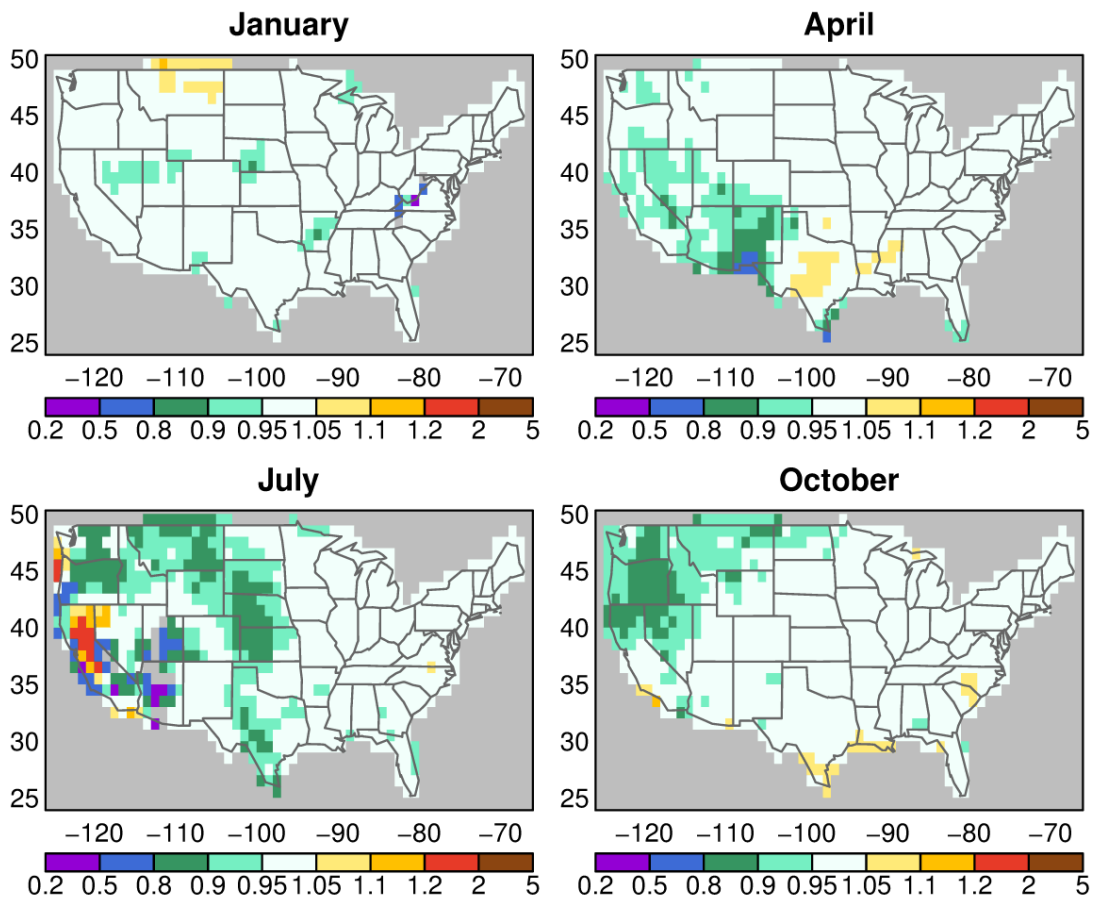
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Figure 3. Illustration of how bias correction can alter the model-predicted future change in precipitation, shown for December using CCSM4. Left column: the observations, model simulation over the historical period (1976-2005; mm/day), and model error over the historical period with respect to observations without any bias correction (%). Right part of figure: For each of the four bias correction methods indicated, shown are the model error with respect to observations over the historical period after bias correction has been applied (%), the model-predicted change in future (2070-2099) precipitation field after bias correction with the indicated method (%), and the amount that the bias correction method alters the original model-predicted change in precipitation between the future and historical period (percentage points).

/cir1/cmip5_regrid/compare_BC_methods_v3_ccsm4.R.ps



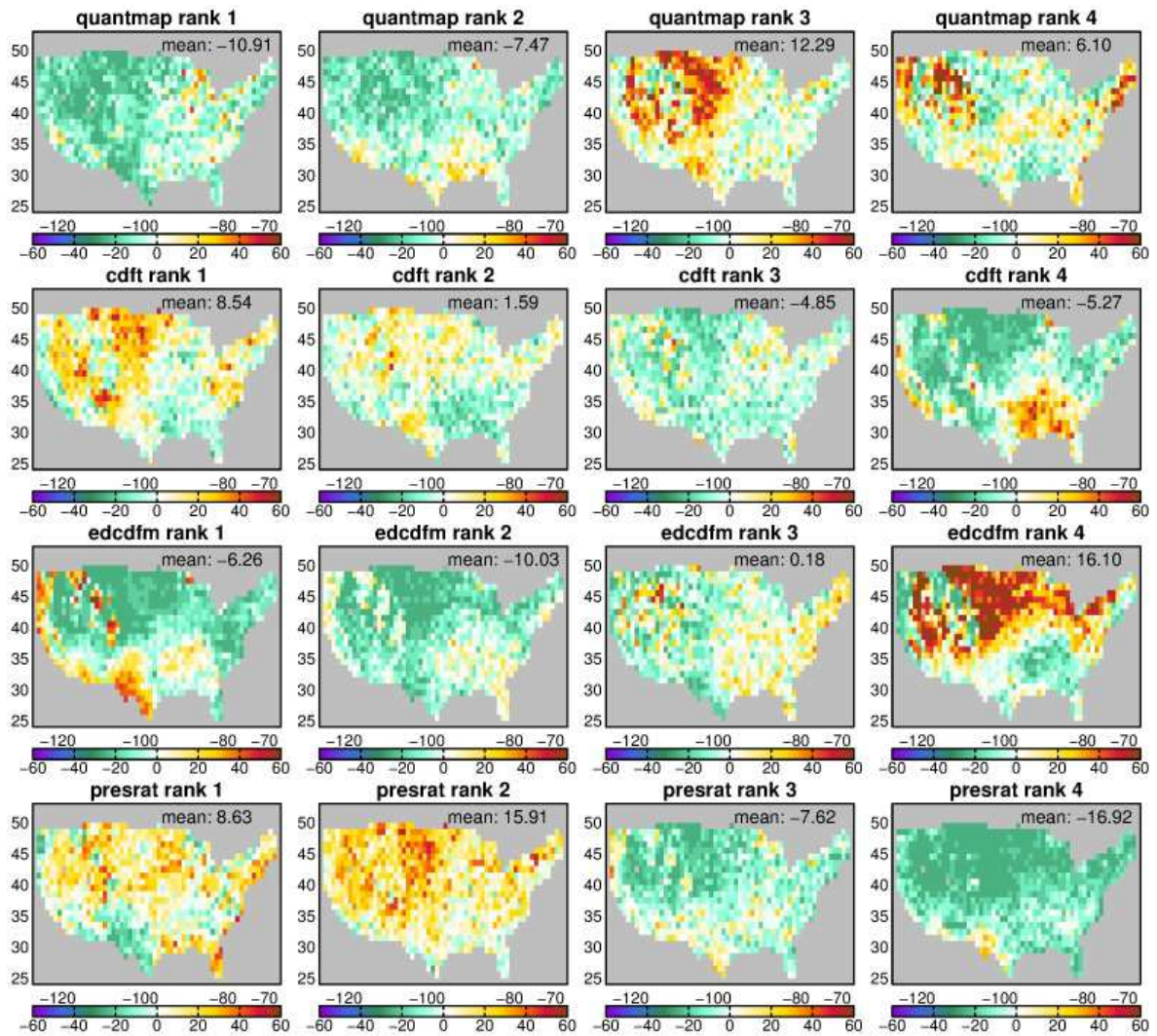
1098

1099 Figure 4. Correction factors, K , for the PresRat scheme that are necessary to preserve
 1100 model-predicted changes (2070-2099 vs. 1976-2005) in mean precipitation, illustrated for four
 1101 months. Values are averaged across 21 GCMs. White areas are within 5% of unity.

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1103 `plot_presrat_factors_allmods.R.gif`

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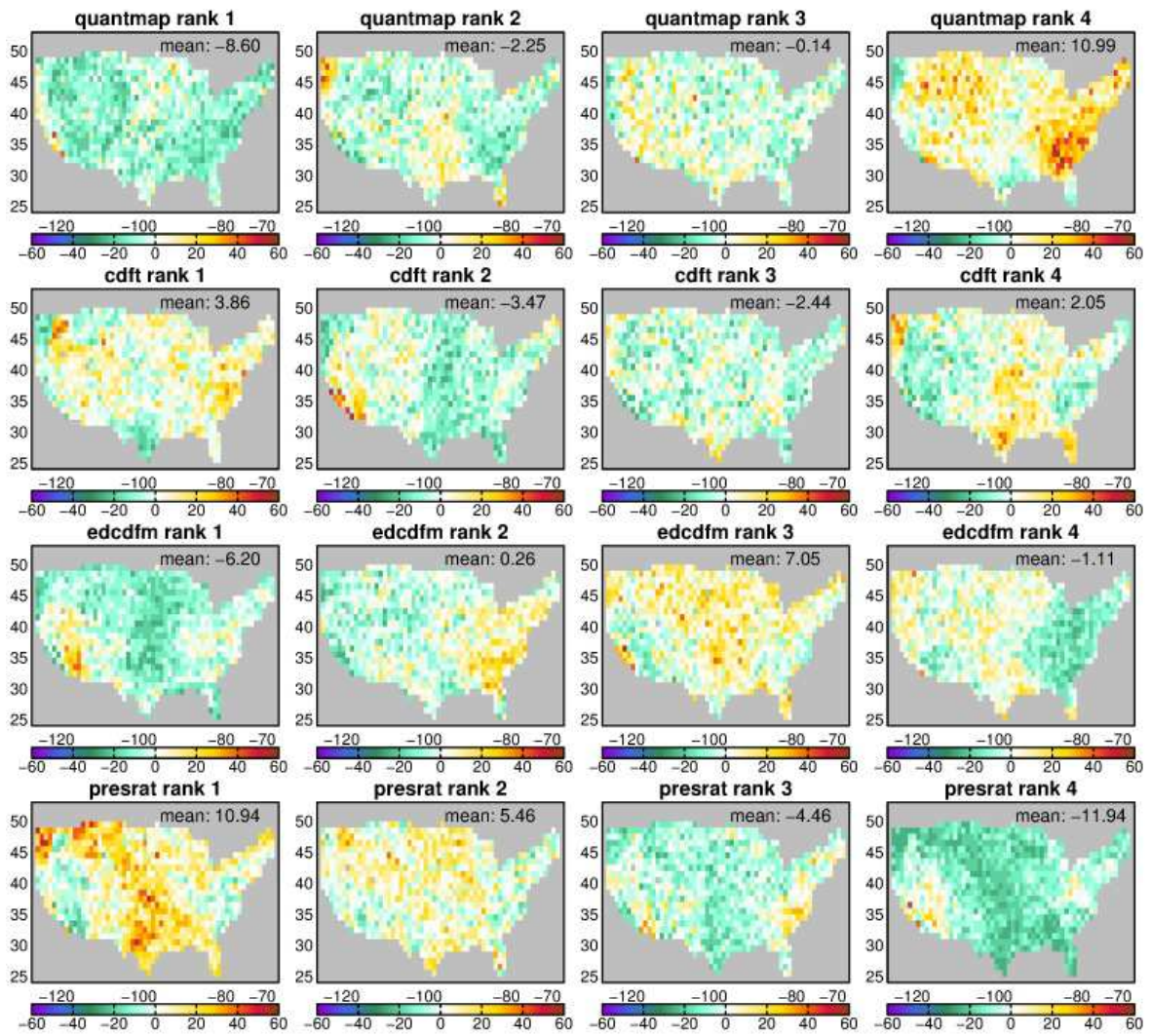
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Figure 5. Percent of the 21 GCMs in which the indicated bias correction method (rows) produces a winter (DJF) 95th percentile daily precipitation value of the indicated rank (columns; 1=smallest value across the bias correction methods; 4=largest). Plotted values are relative to 25%, which is the expected value assuming all 4 bias correction methods produce extrema of equal magnitude. Yellows and reds show where a particular bias correction method produces more values of the indicated rank than expected; greens and blues show where it produces less values of the indicated rank than expected.

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compare_BC_method_ptiles_pctextr_v3.R

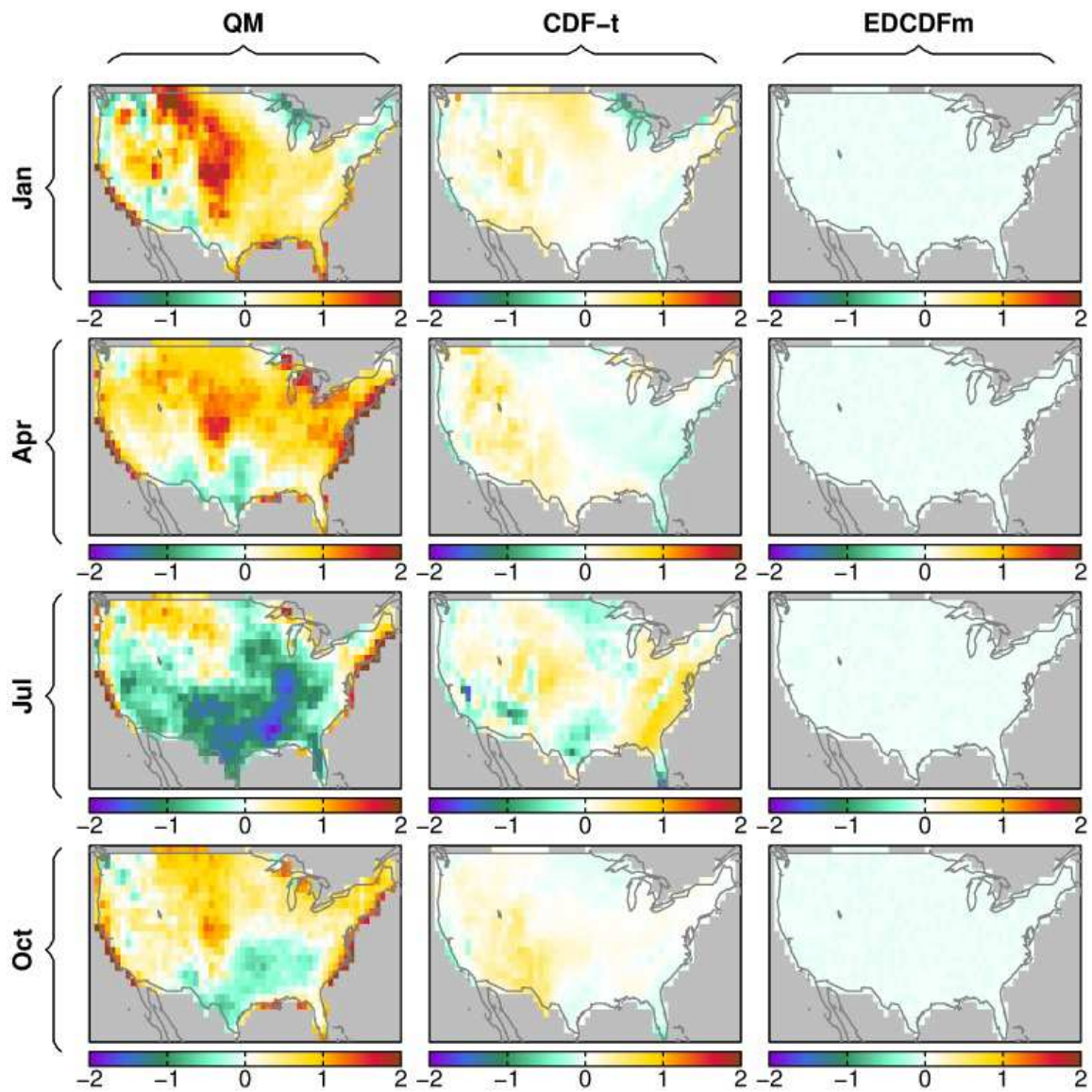


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Figure 6. Same as Figure 5, but for summer (JJA).

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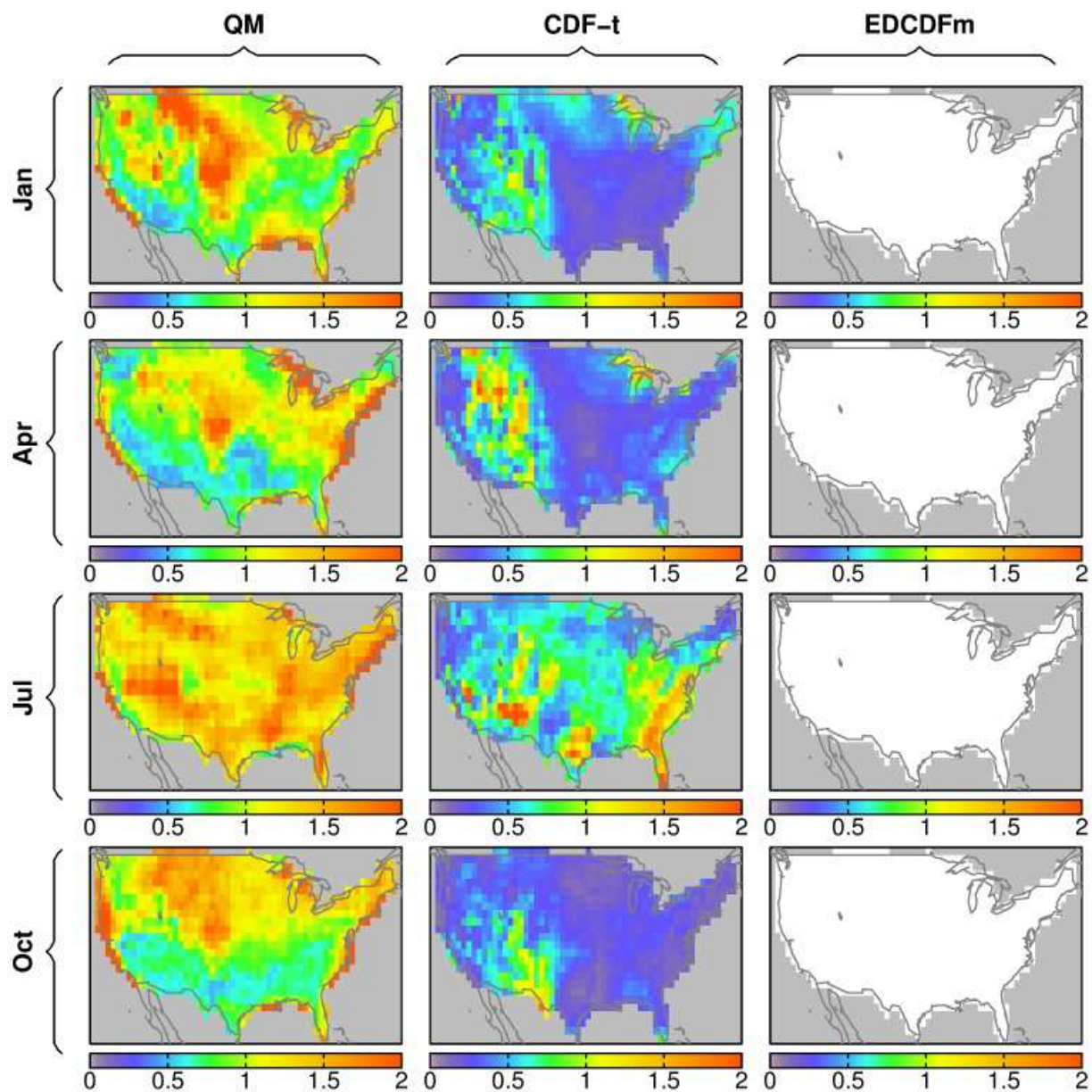


1118

1119 Figure 7. Bias corrected minus original GCM change in daily maximum temperature
 1120 ($^{\circ}\text{C}$) over the period 2070-2099 relative to 1976-2005, shown for 4 months (rows) and 3 bias
 1121 correction methods (columns). Values are ensemble averaged across all 21 GCMs.

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1123 compare_BC_methods_allmods_tasmax_summary_v2.R.ps



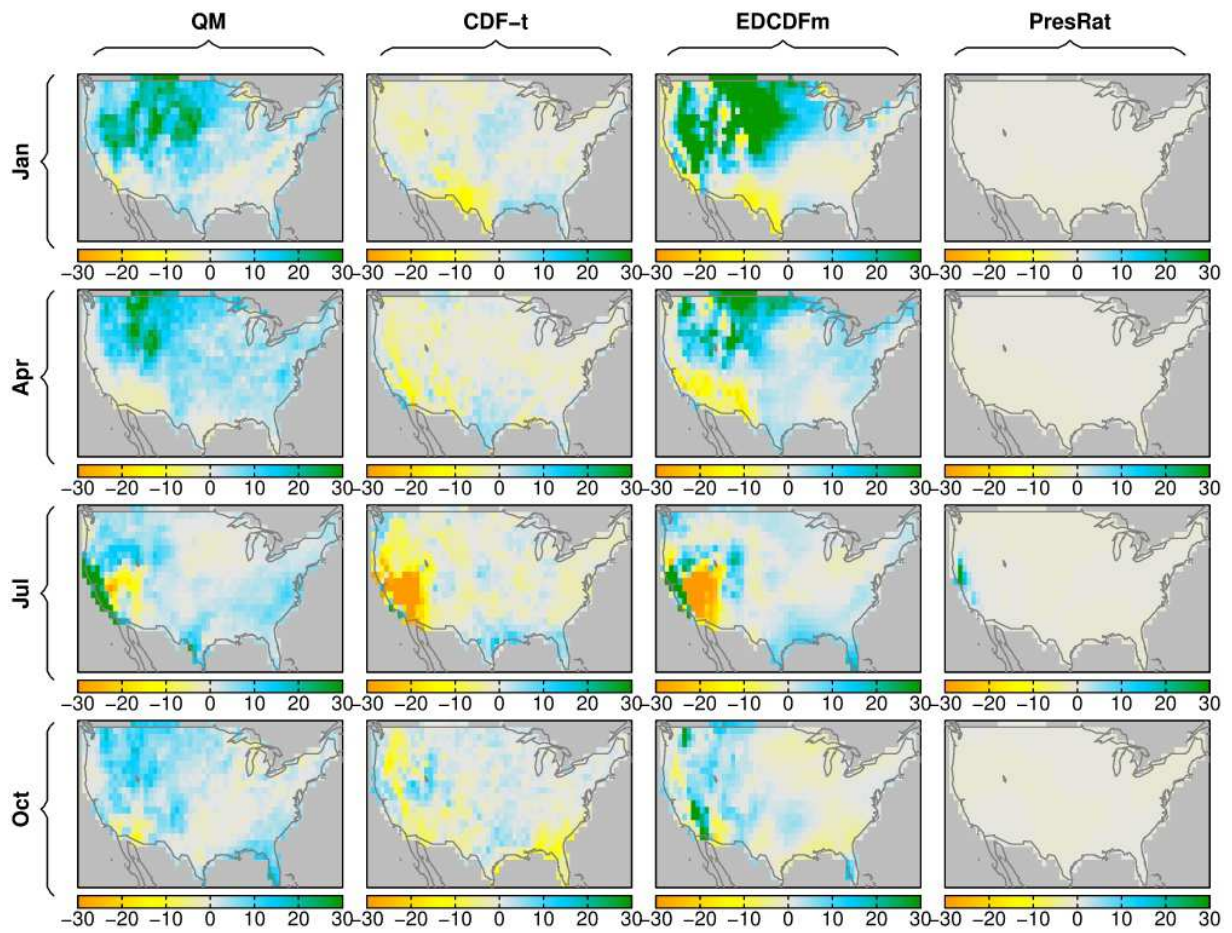
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Figure 8. As in Figure 7, but for the RMS difference (°C), obtained from 21 models, between the original model-predicted future change in daily maximum temperature and the model-predicted change after bias correction has been applied.



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Figure 9. How bias correction alters model-predicted change in future daily precipitation (percentage points), shown for 4 months (rows) and 3 bias correction methods (columns). Values are ensemble averaged across all 21 GCMs.

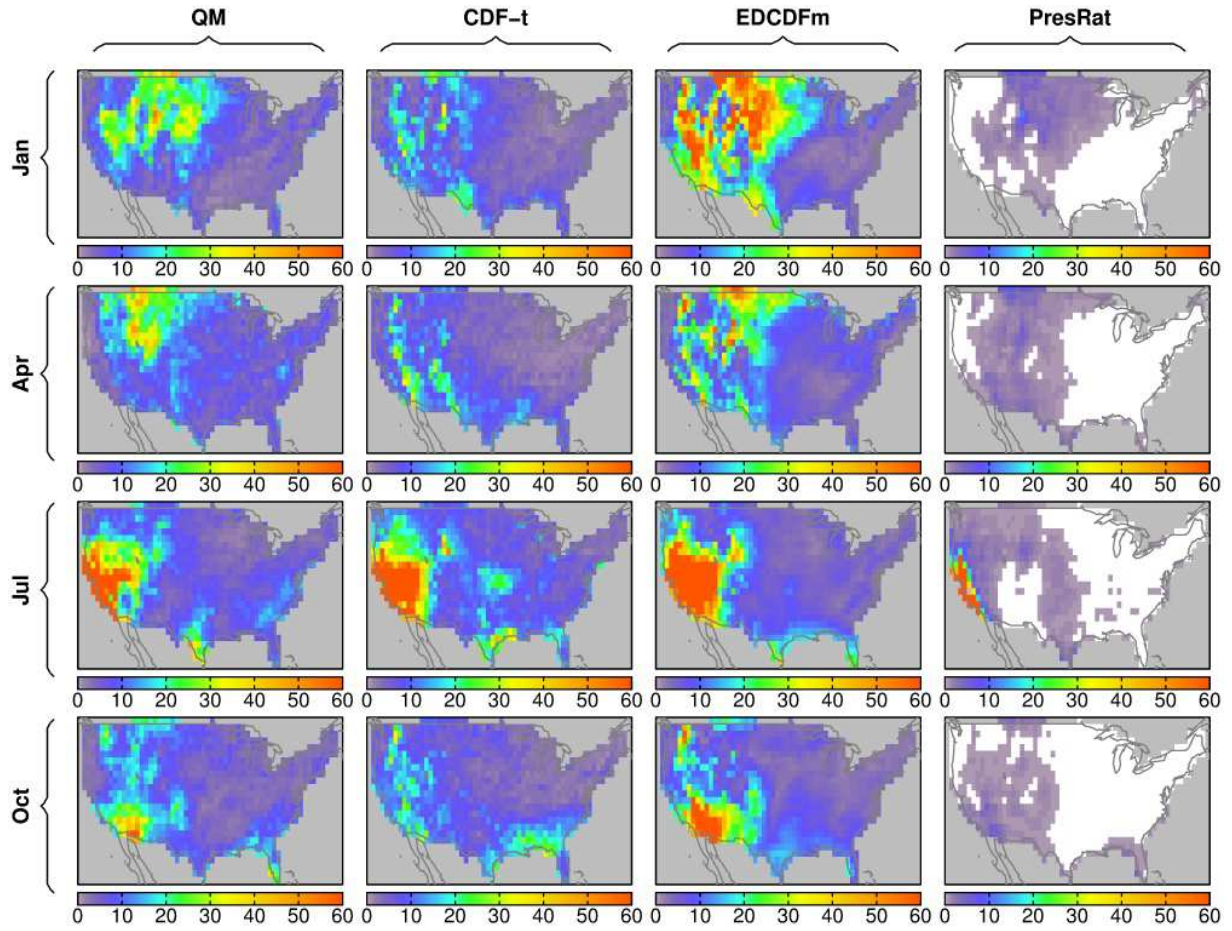
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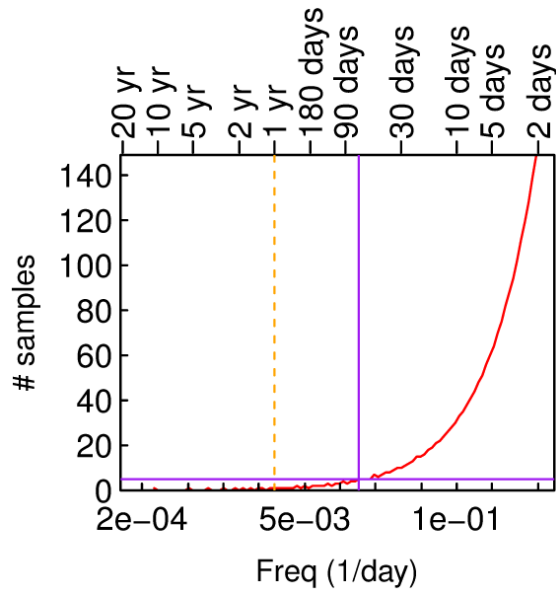
compare_BC_methods_allmods_pr_summary_v2.R

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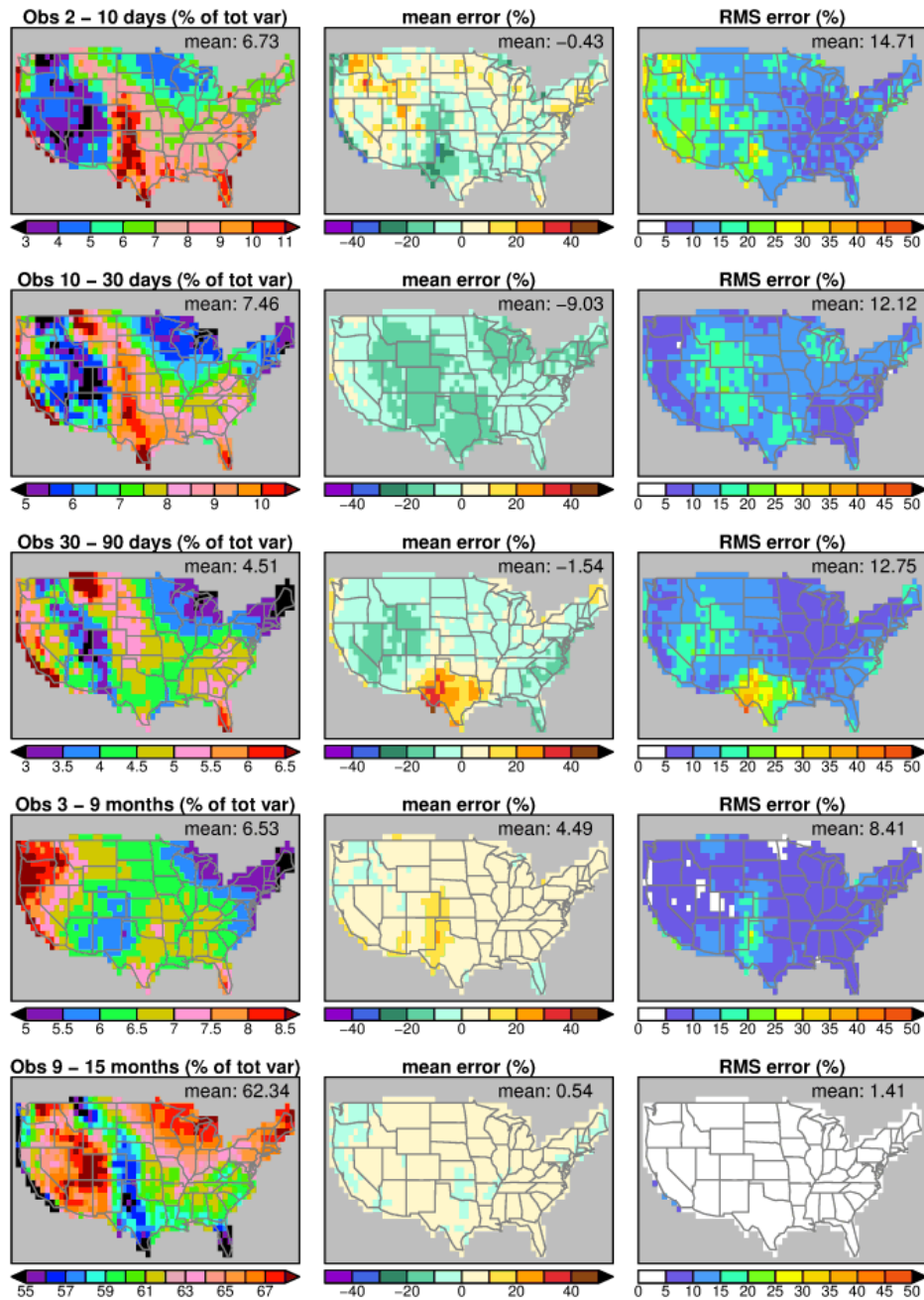
1136

1137 Figure 10. As in Figure 9, but for the RMS difference (percentage points) between the
1138 original model-predicted future change in daily precipitation and the model-predicted change
1139 after bias correction has been applied.



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1141 Figure 11. Number of samples per constant-width bin in the logarithm of frequency. The
 1142 period corresponding to the frequency is shown along the top axis. The vertical dashed orange
 1143 line shows the annual cycle. The purple lines show that the number of samples per logarithmic
 1144 frequency bin exceeds 5 at periods less than about 80 days.



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Figure 12a. Left column: proportion (%) of total variance of daily maximum temperature that falls in the frequency band whose period is indicated in left hand column, from observations over the period 1976-2005. Note that the color range varies substantially by frequency band.

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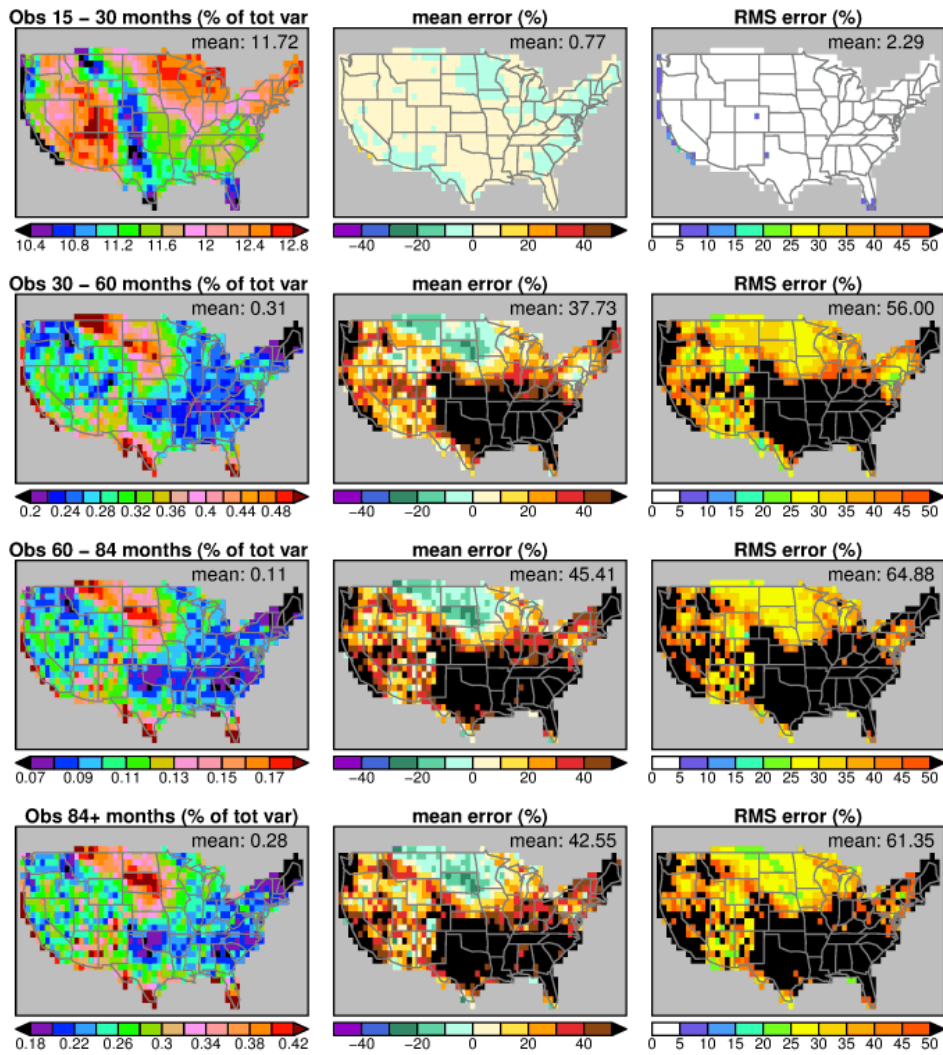
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Middle column: the multi-model mean error (%) for the same quantity in the GCMs, relative to the observations. Right column: the multi-model RMSE (%). Figure continues.

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compare_spec_mod_vs_obs_norm_tasmax_summary_v3.R

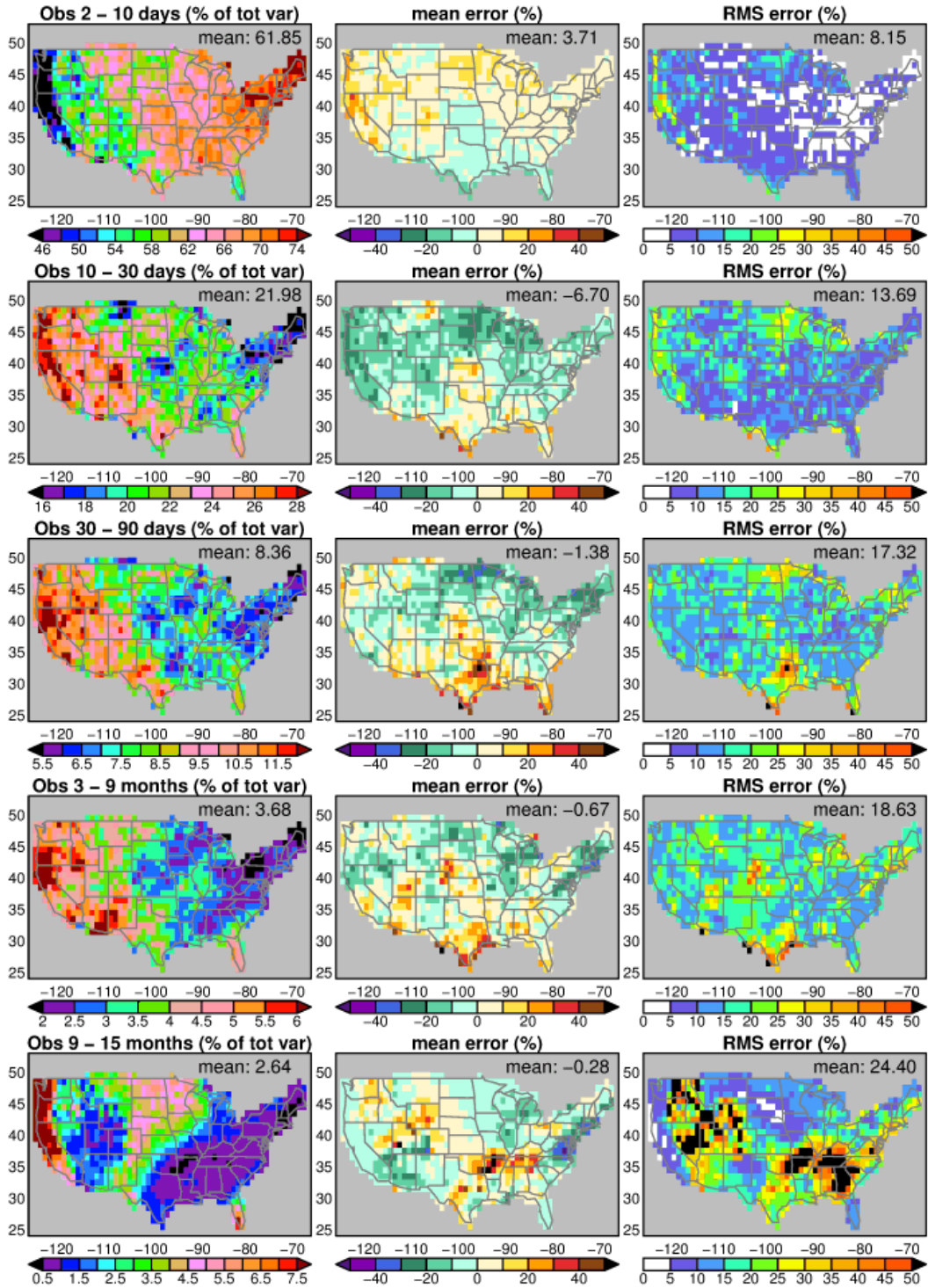


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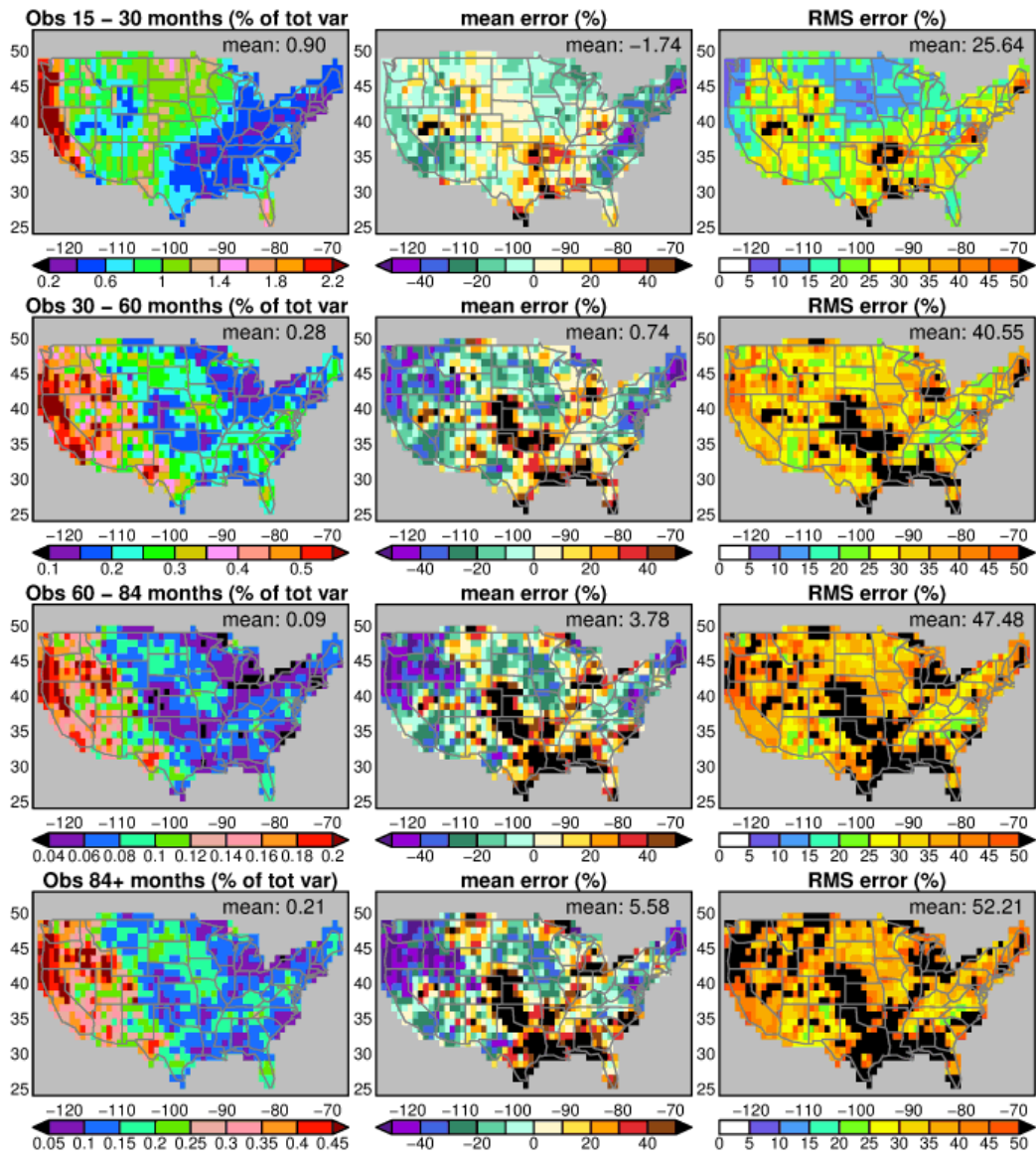
Figure 12b. As in Figure 12, but for frequency bands whose periods are indicated in left hand column.



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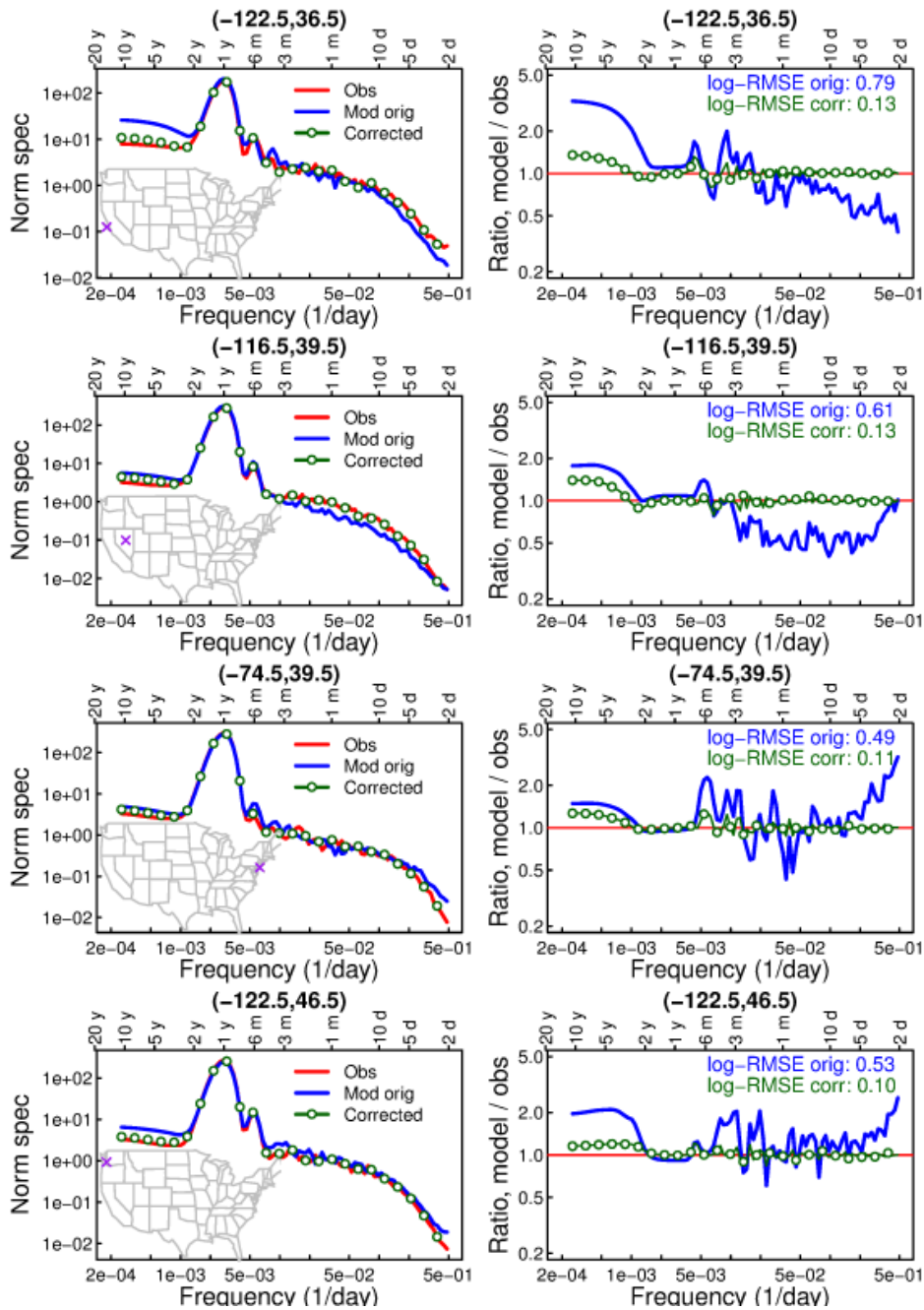
Figure 13a. As in Figure 12a, but for daily precipitation. Figure continues.



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Figure 13b, continued.



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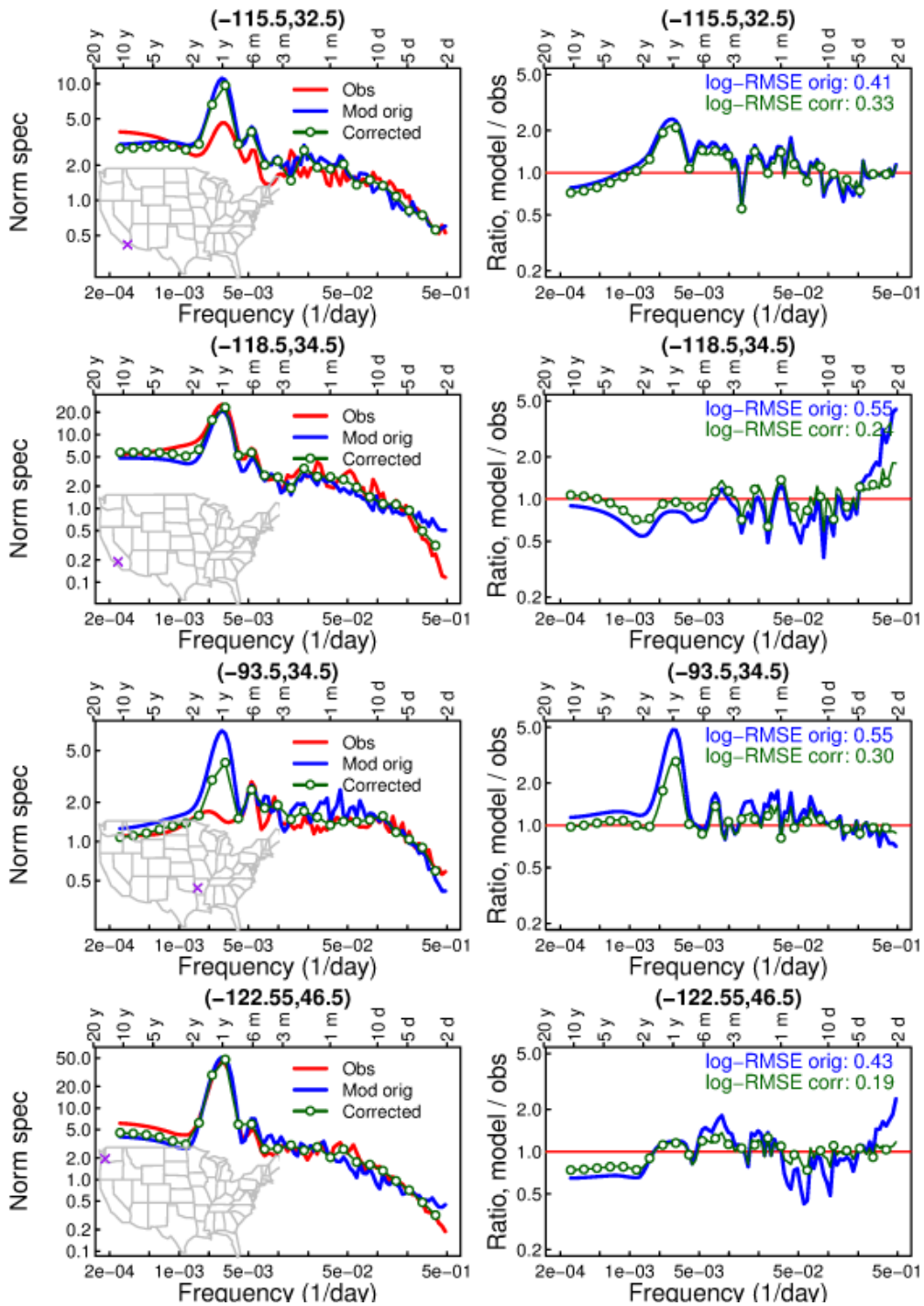
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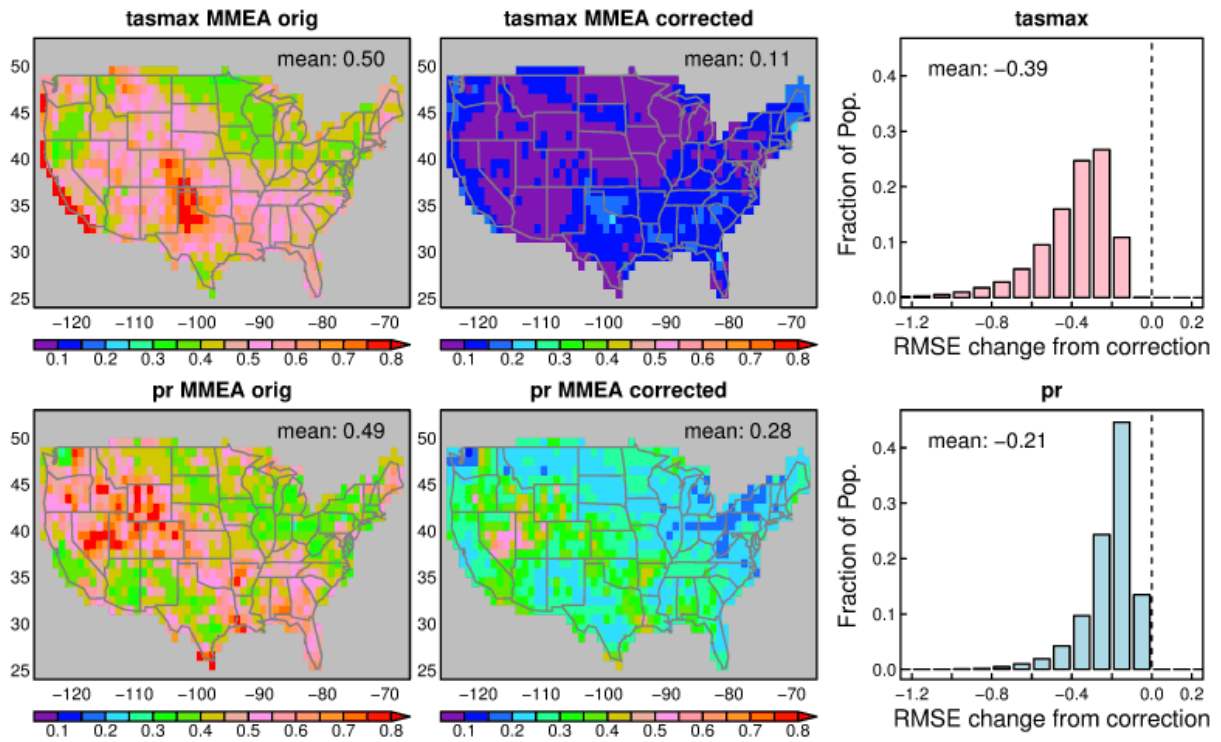
Figure 14. Left column: Normalized spectra of daily maximum temperature from observations (red line), CCSM4 (blue line), and CCSM4 after frequency-dependent bias correction (green dots and line), taken at the location indicated by the purple cross on inset map, coordinates given in the panel title. Right column: Ratio of CCSM4 spectral power to observations (blue line) and ratio of CCSM4 to observations after frequency-dependent bias correction to observations (green dots and line).



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Figure 15. Same as Figure 14, but for daily precipitation.



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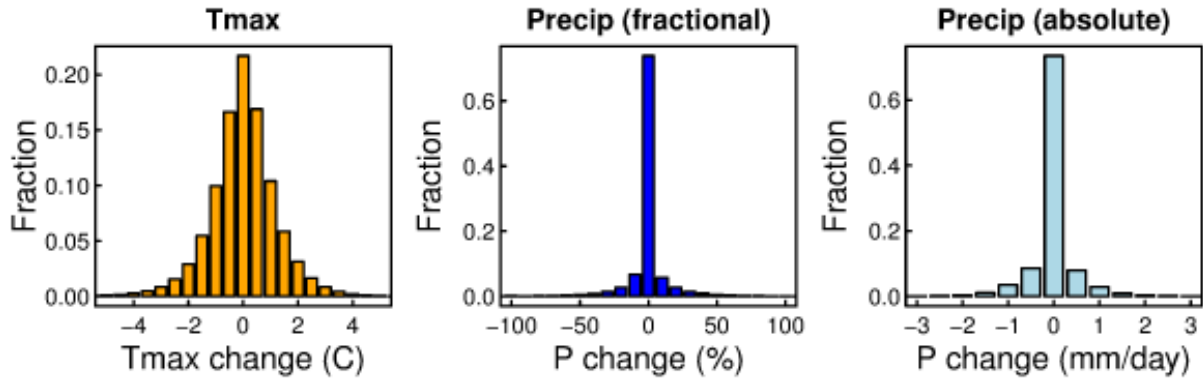
1169 Figure 16. For daily maximum temperature (top row) and precipitation (bottom row), the
 1170 multi-model ensemble average log-RMSE in simulating the observed distribution of variance
 1171 across frequency, both before the frequency-dependent bias correction (left column) and after
 1172 (middle column). Right: histograms of how the frequency-dependent bias correction changes the
 1173 log-RMSE, taken over all models and all locations.

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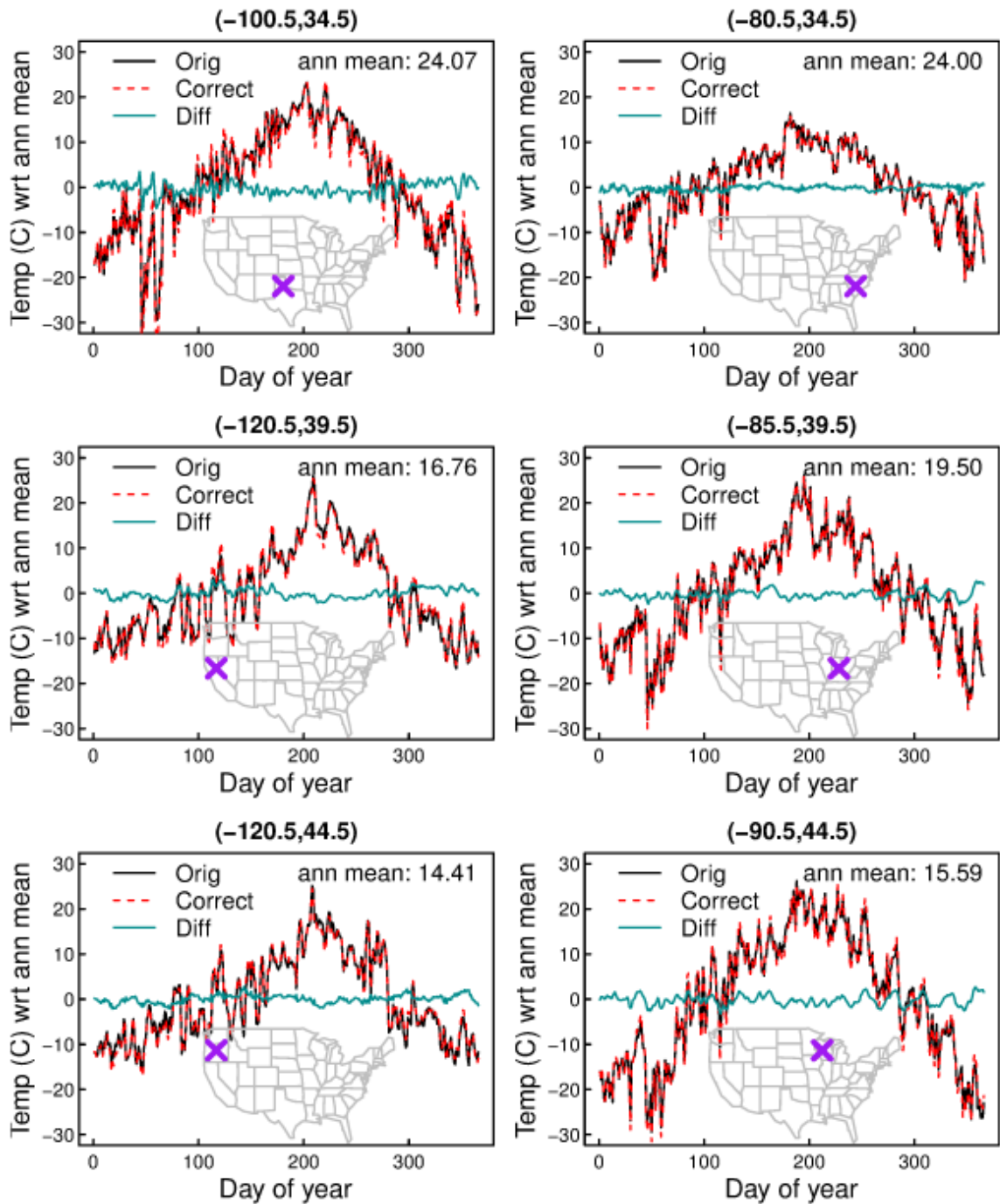
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Figure 17. Histograms of how much the frequency-dependent bias correction alters the daily temperature (left, °C) and precipitation (right two panels). The precipitation results are given both as the fraction change (%) and absolute change (mm/day). Results are shown for all the models across all points in the conterminous U.S.



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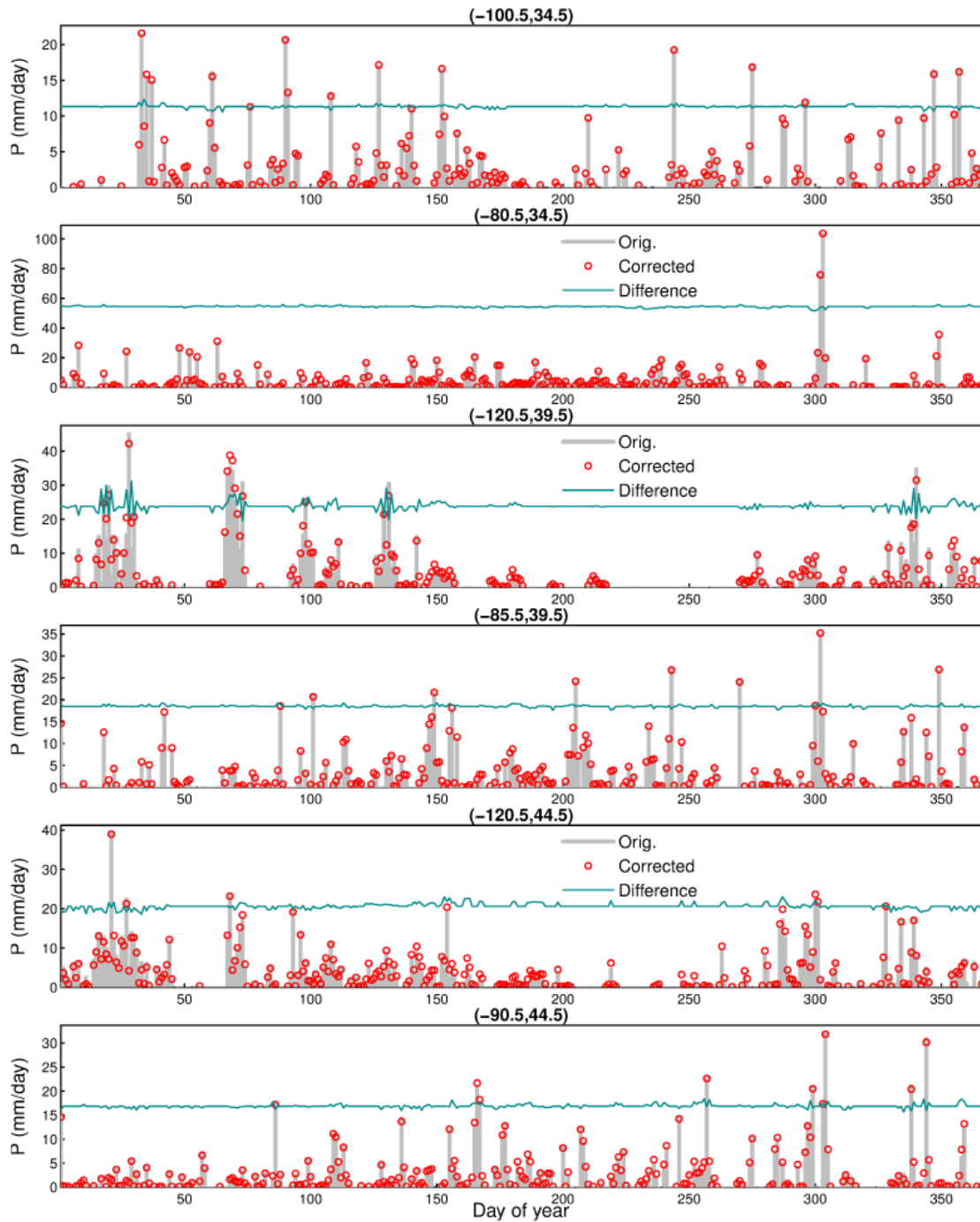
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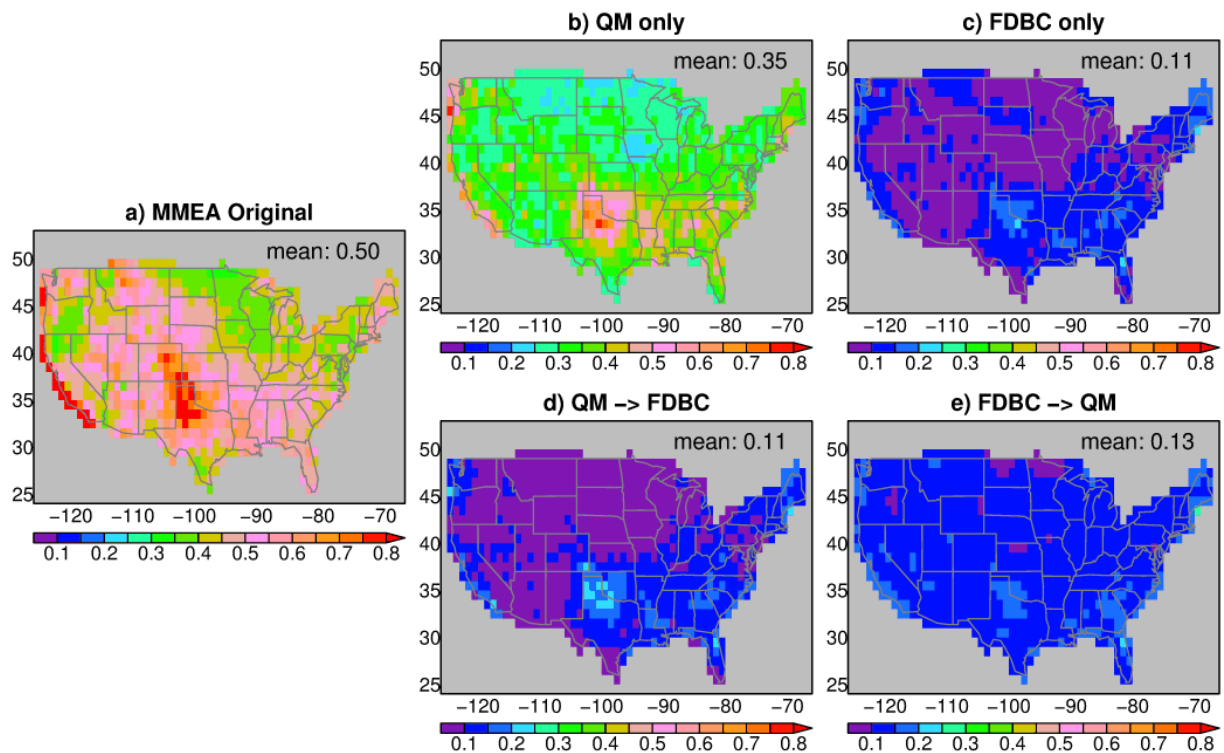
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Figure 18. Example one-year time series of daily maximum temperature at the location marked by the purple 'X' both before (black line) and after (dotted red line) the frequency-dependent bias correction. Values have had the annual mean removed; the value of the annual mean is shown in the upper right part of the panel. The blue line is the time series of the correction, i.e., the corrected time series minus original. Values are from CCSM4 in year 2000.



1188

1189 Figure 19. Example one-year time series of daily precipitation at the location indicated in
 1190 the panel title (longitude, latitude), both before (grey lines) and after (red circle) the frequency-
 1191 dependent bias correction. The blue line is the time series of the correction, i.e., the corrected
 1192 time series minus original, with no scaling but offset to be vertically centered in the middle of the
 1193 panel. Values are from CCSM4 in year 2000.



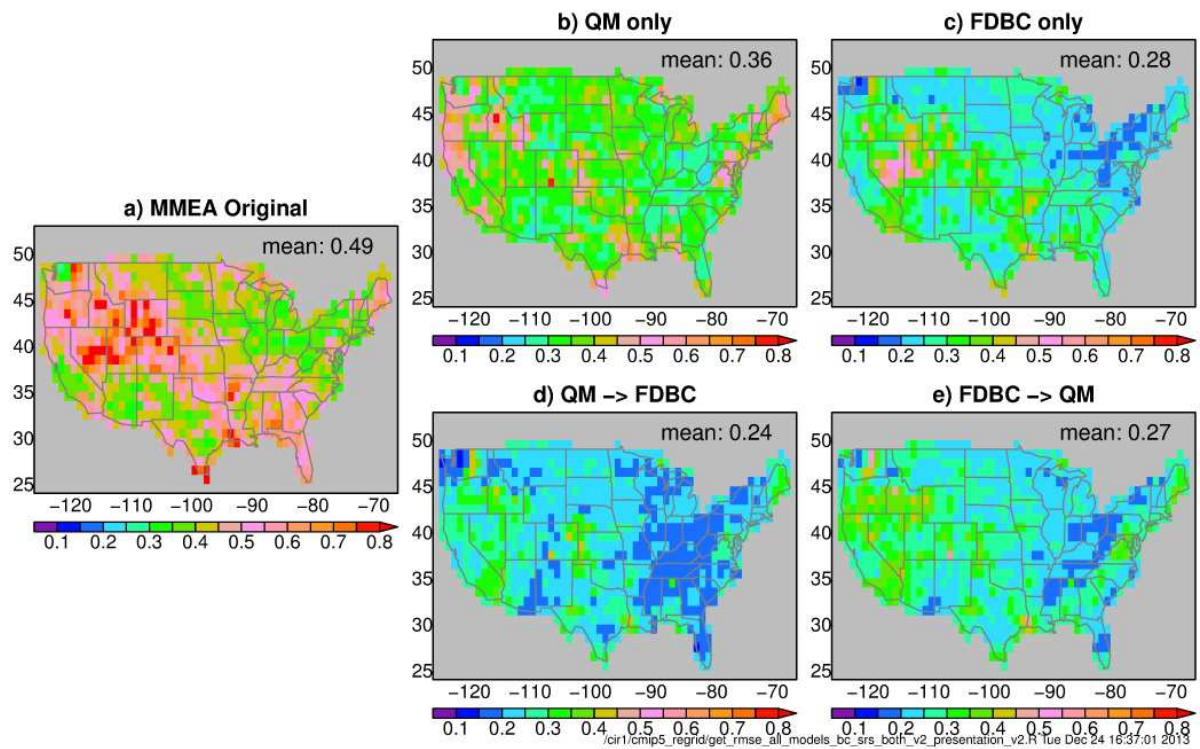
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1195 Figure 20. Multi-model ensemble mean log-RMSE for daily maximum temperature. a)
 1196 the multi-model ensemble average value before any bias correction has been applied. b) With
 1197 only quantile mapping (QM) applied. c) With only frequency-dependent bias correction (FDBC)
 1198 applied. d) With QM applied first, then FDBC. e) With FDBC applied first, then QM.

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get_rmse_all_models_bc_srs_both_v2_presentation.R



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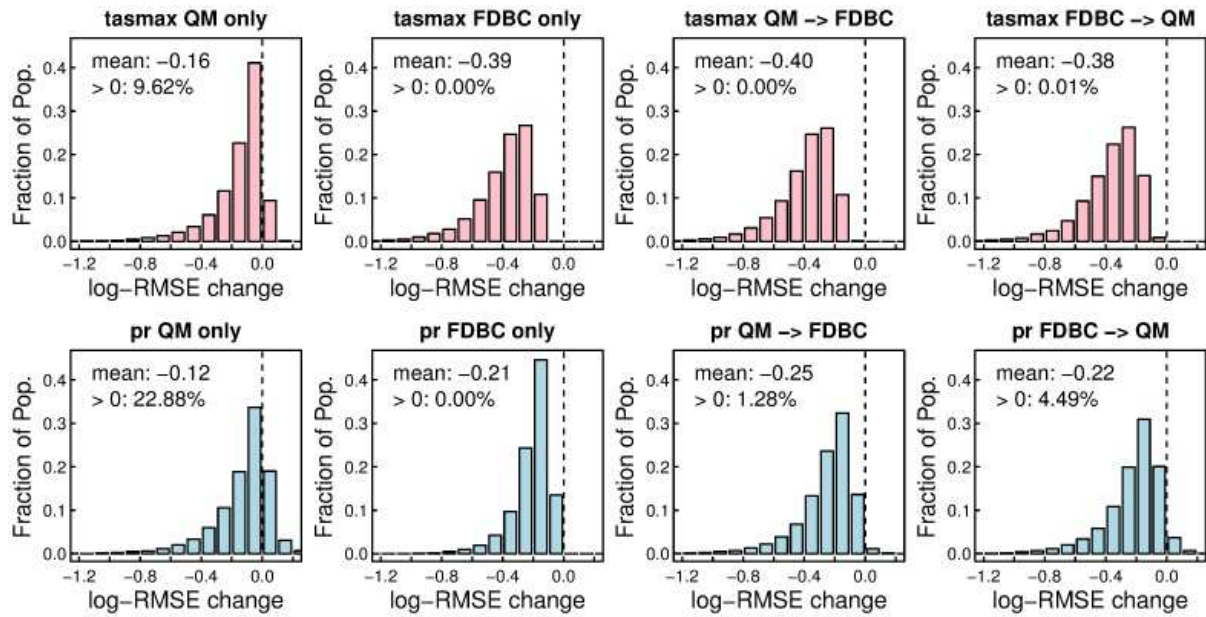
Figure 21. As in Figure 20, but for daily precipitation.

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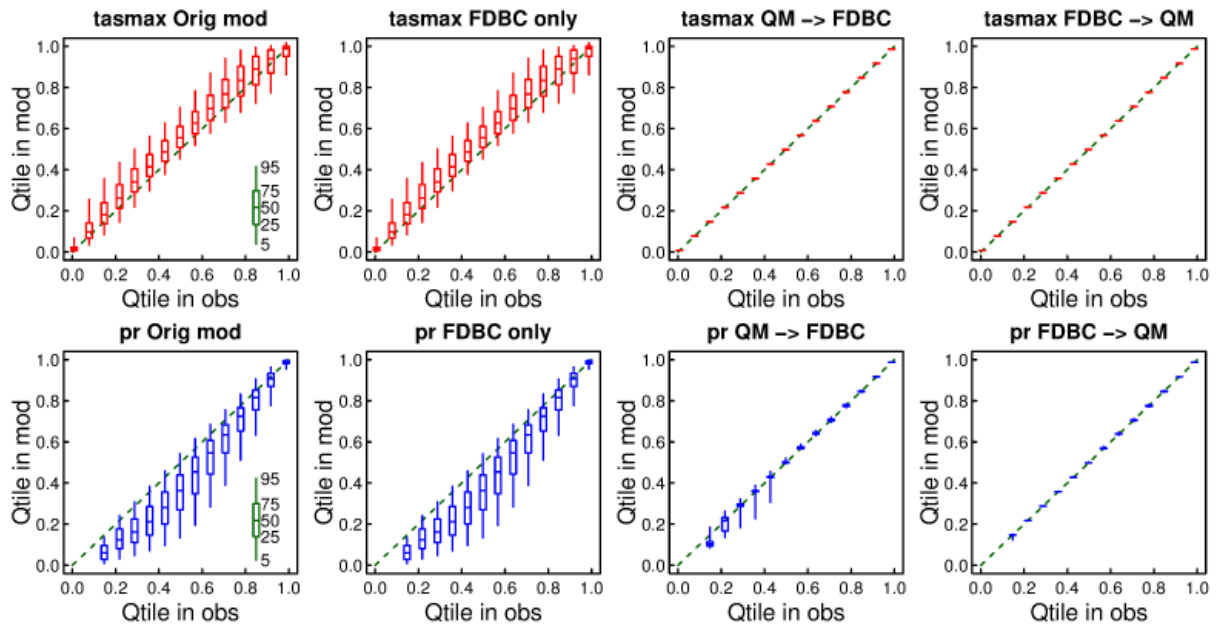
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Figure 22. Histograms of the change in log-RMSE for the models' simulation of the variance spectra of daily maximum temperature (top row) and precipitation (bottom row) when the indicated bias correction method is applied. QM: quantile mapping. FDBC: frequency-dependent bias correction. Also indicated in each panel are the mean value and percent of values greater than zero. Values are pooled over all models and locations.

get_rmse_all_models_bc_srs_both_v2_presentation_hists.R.ps



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1215 Figure 23. Quantile-quantile plots showing how well the GCMs simulate the distribution
 1216 of daily maximum temperature (top) and daily precipitation (bottom), both before (left column)
 1217 and after various combinations (described in Figure 19) of quantile mapping (QM) and
 1218 frequency-dependent bias correction (FDBC). In each panel the dotted green line shows a 1-to-1
 1219 relationship, which would be perfect agreement between the model and observations. The box
 1220 and whiskers show the distribution of model quantile values as indicated in the legend, pooled
 1221 across all models and all locations. Values are obtained from the control period, 1976-2005.

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1223 `get_rmse_all_models_bc_srs_both_v2_presentation_QQ.R.gif`